

Type 2 Vague Events and Their Applications

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(Summary):

Uemura (1991) discovered a mapping formula for Type 1 Vague events, and presented an alternative problem as an example of its application. Since it is well known that the alternative problem results in sequential Bayesian inference, the subsequent research flow is to make the mapping formula multidimensional, to derive the Markov (decision) process by introducing the concept of time, and so on. Furthermore, the stochastic differential equation from which it is derived was formulated. (Hori, Takemura, Matsumoto (2019)) This paper refers to Type 2 Vague events based on the secondary mapping formula. This quadratic mapping formula gives a certain rotation to a non-mapping function by transforming it with a relationship between the two mapping functions. Furthermore, here we refer to the derivation of the Type 2 Vague Markov process and the initial and stop conditions for its rotation.

Date of Submission: 16-06-2021

Date of Acceptance: 01-07-2021

I. Introduction

Uemura (Japanese Buddhist name Hori) (1991) discovered the official mapping. It is sometimes called Vague because it is distinguished from the fuzzy logic of Zadeh (1965). Therefore, our study was named Vague Sets and Theory (Hori, Takemura, Matsumoto (2019)). Zadeh's fuzzy deals with vertical ambiguity, while our Vague deals with horizontal ambiguity. Also, Zadeh's modeling is conceptually very close to the interval modeling of subjective Bayesian theory, and the rotation based on our quadratic mapping formula is very related to factor analysis or independent component analysis (Hori, 2020). Our study image is eye. From our moving eye, we can obtain our feeling on our decision. As our feeling is some factor in this case, it is the vague factor. Therefore, our study can analysis this vague factor.

II. Type 2 (fuzzy) Markov process

Uemura (1991) obtained the type 1 mapping formula (1) on some function $f(x)$ by $g_1(x)$. However, here, an alternative problem was shown as an application example. Later, it is shown to be a theorem (Hori, Takemura, Matsumoto (2019)).

$$SUP_{y=f(x)} \quad g_1(x) = g_1(f^{-1}(y)) \quad (1)$$

Next, Hori (maiden name Uemura) (2020) formulated the formula for the secondary mapping as in equation (2).

$$SUP_{y=f(x)} \quad g_2(Z) = g_2(g_1^{-1}(f^{-1}(y))) \quad (2)$$

$$Z=g_1(f^{-1}(y))$$

Here, in Eq. (2), it is the formula of the quadratic mapping that maps Eq. (1) again with. A notable property in the quadratic mapping formula is that when the mapping functions are equivalent as in Eq. (3), they are inverted 180 degrees. This indicates that it is a kind of main factor analysis. Here, in the main factor analysis, 180 degree rotation requires two rotations every 90 degrees. However, note that the formula for the secondary map is flipped 180 degrees in a single rotation. $g_2(x)$

$$if \quad g_1(\cdot) = g_2(\cdot), \quad then \quad x = f^{-1}(y) \quad (3)$$

Next, assuming that the transition matrix is L , the Markov process is formulated as follows (Takahashi, 2011). D_t

$$D_t = L(t, x_t) \quad (4)$$

Finally, the type 1 Markov process that introduced the concept of Vague is derived by equation (5), and the type 2 Markov process is derived by equation (6).

$$F_t = L^{-1}(t, g_1(x_t)) \quad (5)$$

$$F_{F_t} = \begin{matrix} SUP \\ \{y_t=L^{-1}(t, g_1(x_t))\} \end{matrix} L^{-1}(t, g_2(x_t)) \quad (6)$$

$$= L^{-1}(t, L^{-1}(t, g_2(g_1^{-1}(f^{-1}(y_t))))$$

III. Initial condition and stop condition

The initial and stop conditions for a normal Markov process are shown in (Takahashi, 2011). Since we are dealing with horizontal ambiguity, we introduce the concept of two-dimensional Possibility Theory (Dubois, Parade (1988)). The initial conditions and stop conditions are shown in Eqs. (7) and (8), respectively.

$$\begin{aligned}
 (1) & (F_{10t}, F_{20t}) = (Z_{10t}, Z_{20t}) \quad (7) \\
 (2) & POS((F_{1t}, F_{2t}) \geq (Z_{1t}, Z_{2t}) | x_0) \leq POS((DF_{1t}x_0, DF_{2t}x_0) \geq (DZ_{1t}x_0, DZ_{2t}x_0)) \\
 (3) & NES((F_{1t}, F_{2t}) \geq (Z_{1t}, Z_{2t}) | x_0) \geq NES((DF_{1t}x_0, DF_{2t}x_0) \geq (DZ_{1t}x_0, DZ_{2t}x_0)) \\
 & \text{here } (DF_{1t}x_0, DF_{2t}x_0) = (DX_{1t}, DX_{2t}) \\
 *F_{10}(\cdot)_t &= F_{20}(\cdot)_t \quad (8) \\
 (1) & F_{ti0} = Z_{ti0} (i = 1,2) \\
 (2) & POS(F_{it} \geq Z_{it} | x_{i0}) \leq POS(DF_{xi0} \geq DZ_{xi0}) (i = 1,2) \\
 (3) & NES(F_{it} \geq Z_{it} | x_{i0}) \geq NES(DF_{xi0} \geq DZ_{xi0}) (i = 1,2) \\
 & \text{here, } DF_{xi0} = DZ_{xi0} (i = 1,2)
 \end{aligned}$$

Here, represents two vague events, and a two-dimensional possibility theory is applied. If the mapping functions have the same value, they are inverted 180 degrees, and the initial condition and the stop condition are inverted. Note that in this case, the Vague event is also one. $F_{i0t}DF_{i0t} (i = 1,2)$

$$\begin{aligned}
 (1) & (F_{1t0}, F_{2t0}) = (Z_{1t0}, Z_{2t0}) \quad (9) \\
 (2) & POS((F_{1t0}, F_{2t0}) \geq (Z_{1t0}, Z_{2t0})) \leq POS((DF_{10}, DF_{20}) \geq (DZ_{10}, DZ_{20})) \\
 (3) & NES((F_{1t0}, F_{2t0}) \geq (Z_{1t0}, Z_{2t0})) \geq NES((DF_{10}, DF_{20}) \geq (DZ_{10}, DZ_{20})) \\
 & \text{here } (DF_{10}, DF_{20}) = (DZ_{10}, DZ_{20})
 \end{aligned}$$

$$\begin{aligned}
 F_{10}(\cdot)_t &= F_{20}(\cdot)_t \quad (10) \\
 (1) & F_{ti0} = Z_{ti0} (i = 1,2) \\
 (2) & POS(F_{it} \geq Z_{it}) \leq POS(DF_{i0} \geq DZ_{i0}) (i = 1,2) \\
 (3) & NES(F_{it} \geq Z_{it}) \geq NES(DF_{i0} \geq DZ_{i0}) (i = 1,2) \\
 & \text{here } DF_{i0} = DZ_{i0}
 \end{aligned}$$

IV. In Conclusion

In this paper, we mention the type 2 Markov process and derive the initial condition and the stop condition from the two-dimensional possibility theory. A future task is to formulate a stochastic differential equation that derives the formula for the quadratic mapping. Finally, the quadratic mapping formula can be regarded as a multidimensional nonlinear factor analysis and is closely related to the field of artificial intelligence.

(Reference)

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