

## Technical Evaluation for connections of Non-standard Vector Groups (Dy5/Dy11 and Yyn) in Nigerian 33/11kV Network

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**Abstract:** Evolving from the era of British Standards Specifications to multiplicity of standards, Electricity Industry in Nigeria has witnessed very negative transformations. Efforts of engineers to address the matter over the years has not yielded any dividend because control of equipment specifications for the electricity industry is beyond the control of the engineering community. In this write-up, we have tried as much as possible to take an in-dept look at Transformer Vector Group abuse in Nigeria and its attendant consequences on the entire Power System. Efforts have also been made to address multiple cases of transformers introduced into the system with a view to correct the power system anomalies.

**Background:** One of the key areas of the supply industry that needs conformance to required standard include the ever-elusive power system stability and power quality, and the matter of Transformer Vector Group may be part of the problems. Efforts by the Nigerian Electricity Management Services Agency (NEMSA) in recent years to address this has not really yielded positive result because engineers themselves are still battling with the matter of power availability to think of and understanding other critical areas of Power System Engineering. We are still trying to understand this controversy over transformer vector group and its effect on the power system, denying NEMSA the much-needed voice for this crusade.

**Materials and Methods:** We have endeavoured in this article to take a close look at the Nigerian National Grid in terms of the Distribution Sub-sector and Network integration with a view to addressing issues that can create instability in the 132/33kV Sub-transmission system. To achieve this the problems of the Nigerian National Grid is reviewed through standard Network Configuration requirement from Generation through Transmission to Distribution Electricity Networks, evaluating the attendant issues, analysing transformer Vector Group abuse and addressing the technical implications.

**Results:** The investigation revealed some instability introduced into the Electric Power System with the installation of non-standard transformers and these include unavoidable phase-shifts that cause error when trying to determine the true power consumption, results in deviation of actual power-factor and Real Power delivered, Negative Power Factor that produces reverse power flow in the system and possible over-voltages, the effects of the harmonic currents that results in additional copper losses, Increased core losses, Increased electro-magnetic interference, as well as Resonance between winding reactance and feeder capacitance. The conclusive results show about 35,138.88Kwhr energy deficit per month and 421,666.56Kwhr per year for a 500KVA transformer operating at  $24^{\circ}$  phase-shift due to introduction of Dy11 Power Transformer in the 33/11kV Network.

**Conclusion:** It is concluded that outright ban of such installation is the basic solution to this problem and in cases that are already in the system, internal or external vector re-configuration is recommended.

**KeyWords:** Vector Group, Phase Shift, Dy1, Dy5, Dy11, Yyn, Power Transformer, Distribution Transformer

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### I. Introduction

In electrical power system engineering, vector group is the method for characterizing the high voltage (H.V) and low voltage (L.V) winding connections of three phase transformers, as approved by international electro technical commission (IEC) and other international standards. According to IEC 60076-1 coding technique, vector groups are represented by letters for each set of winding and the phasor related with (H.V) is taken as reference with capital letters and is stationary at 12 0' clock, while (L.V) side vector is rotating with the reference vector using lowercase letters, to represent phase displacement between two sides of transformers.

In a typical power system network like Nigerian National Grid, we will observe quite a number of forward and backward  $30^{\circ}$  phase shifts as shown in figure 1. The reason for the forward and backward  $30^{\circ}$  shift introduced by delta/star or star/delta transformer is that delta connection provides a path for the third order harmonic current in Generator Step-up transformers and hence no distortion because of it. For

Power export/import transformers used for Transmission purpose, Transformer star-star connection may be preferred since this avoids a grounding transformer on generator side and perhaps save on neutral insulation.

Three phase power transformers in transmission may have Y-Delta windings because of economics (Y on HV side to have less insulation requirements per winding and Delta, on LV-high current side for copper savings per phase) or may be used to restrict zero sequence current from Transmission line under fault penetrating into generator circuit. These configurations produce phase shift of 30 degree between HV and LV side before finally being delivered to the end user who must receive an almost lossless replica of power generated at the source. Since there are several voltage transformations from the source to the end user in a typical large grid network, there will be a number of forward and backward 30° phase-shifts as indicated.

## II. The Problems Of Nigerian National Grid

In an effort to eliminate harmonics in the system and maintain the power supply integrity replica of source of generation in the Nigerian Power System, deliberate phase-shift arrangement is made right from generation to distribution levels as shown in figure 1 below. This is because it is easier to correct a phase-shift than dealing with harmonics in the power system. For instance, a close look at the diagram shows several clockwise and anti-clockwise movements in the vector configurations in an effort to maintain true image of the source. However, it has been observed that several varying vector group configurations at variance with these standard requirements have been introduced into the system nationwide and we need to take a close look at the implications and proffer possible solution. **This is the object of this write-up.**

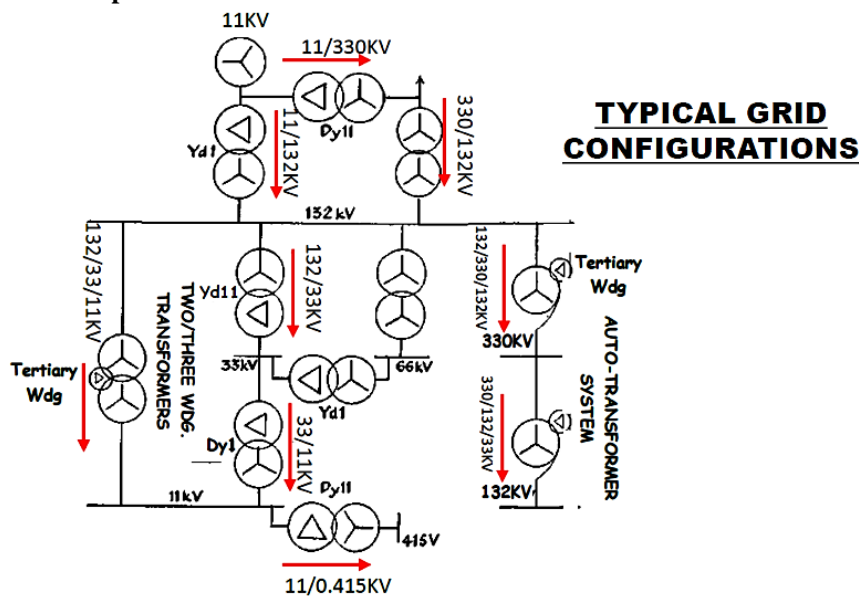


Figure 1: Vector-group Configuration in Nigerian National Grid

This is the basis for Nigerian Electricity Supply and Installation Standards Rules (NESIS 2015 2.3.4.1 and 4.2.4.1) which give detailed specifications on how these transformations can be achieved.

If these regulations are strictly adhered to, it will result in the phasor relationship between the generation and distribution subsectors of the power system illustrated in the diagrams of figure 2 below.

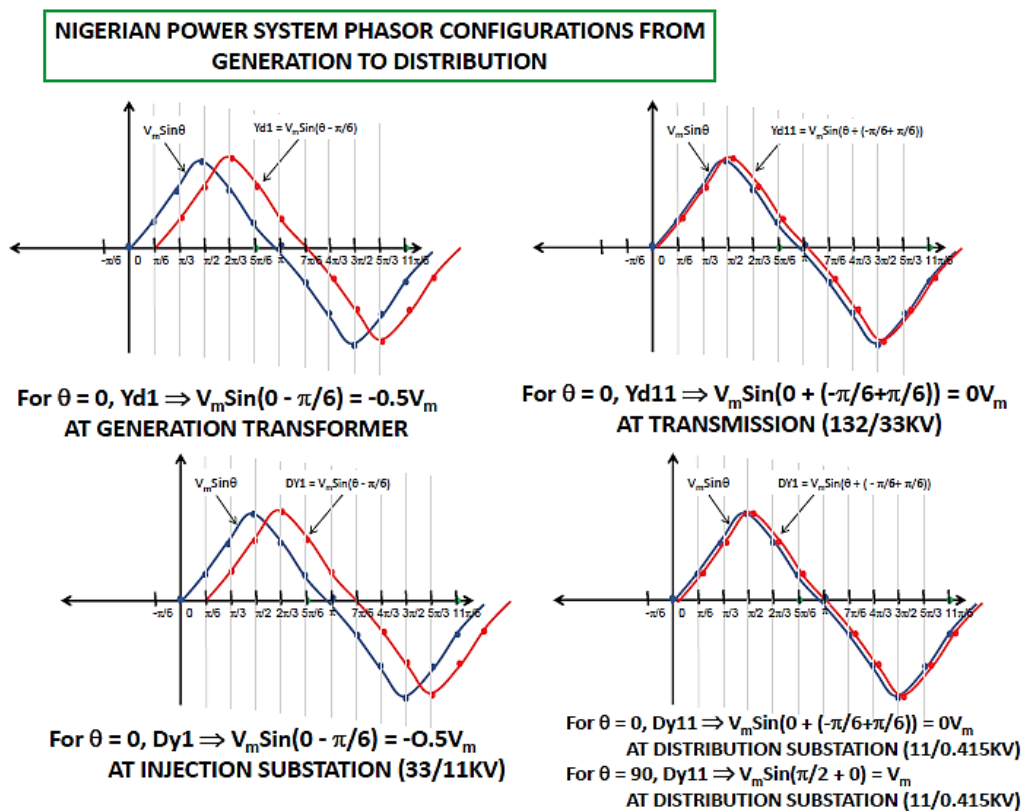


Figure 2: Voltage Wave-form based on the Vector-group Configurations

### III. Problem Evaluation

Several issues of Vector Group abuse in the Nigerian 33/11kV Sub-transmission Network have been discovered of recent. These range from installation of 33/11kV Dy11 Power transformers to Dyn5 11/0.415 Distribution Transformers in place Dy11 as well as 11/0.415 Yyn0 in the 11kV network. We will address these cases one after the other.

#### 3.1 Dy11 Transformers in the 33/11kV Network

It is a well-known fact that so many power transformers of the Dy11 configuration have been introduced into the 33/11kV System by quite a number of establishments without due consideration to attendant technical implications on the National Grid. Application of Dy11 in the 33/11kV system of the National Grid could create a problem in the system, given the Vector Configurations from Generation down to Transmission and subsequently to Distribution levels. Some of the problems introduced include:

1. **Unwanted Circulating Currents** in the system, Out-of-step voltages could adversely affect system operation and stability, Phase-angle displacement conditions may be injurious to the power system in times of faults and critical loads.
2. **Differential Current Control:** There is the introduction of abnormal phase angle displacement that could cause problem to the entire Power System. In this regard, the combination of the Power Transformer in series with the Distribution Transformer where additional  $60^\circ$  phase-shift has been introduced shall be considered as technical insertion of Phase-shifting Transformer in the Power System between Transmission and end users. **This will create serious problems in the Power System Configurations.**

There are Particular differential currents arising from this type of special transformers in backup current circulation.

3. Accuracy of **Metering or Monitoring the amount of Energy** in the circuit in Amplitude and Phase-angle due to additional phase angle difference or phase-shift effect in the connection of the relevant Current Transformers. These include;
  - **Actual Phase Angle Shift ( $\theta$ ) introduced by the transformers**
  - **Star-point location of the Metering Current Transformer**

4. **Unbalance System Considerations** involving possibilities of voltage and current unbalances that can possibly give rise to harmonics. Any deviation in voltage and current waveform from perfect sinusoidal, in terms of magnitude or phase shift is termed as unbalance.
5. **Phase-shift anomalies** arising in the system using the impact of the Delta and the Star connected CTs placed respectively on both the Star and the Delta sides of the transformer as follows:
  - There will be **magnitude matching and differential summation** problems.
  - **Zero sequence currents** (Delta connected CTs) may exist from the grounded Star winding in conflict with the zero sequence free currents measured from the Star connected CTs on the Delta winding of the transformer.
  - **Additional phase shift** may be introduced by the CTs from both sides of the transformer in Star, such that the currents introduced to the relay terminals will have different transformer phase values.

### 3.2 Dy5 Transformers in the 11/0.415kV Network

The Dyn5 and Dyn11 transformer have the same output voltages and phase sequence and the same neutral connection to the secondary star point. The main difference is that the output voltages relative to the neutral are all reversed if we connect one of each transformer to the same supply. When one phase is at maximum positive with respect to neutral on the Dyn5, at the same instant that phase will be at maximum negative on the Dyn11.

### 3.3 Implications of the Vector Group Star-star 3-phase Yyn, 11/0.415KV Transformer connection

There is this case of Yyn, 11/0.415kV Traction Transformers installed along Abuja-Kaduna rail route for the purpose of Railway Communication Systems and Rail-line services by the Chinese Civil Engineering Company for use by Electric Traction. This is illustrated in figure 9 interfaced with 132/33kV source:

## IV. Addressing The Technical Implications

The technical implication of Dy11 connected to the 33kV Network at Injection Substations can be appreciated from the diagrams of figure 3 to figure 6 below.

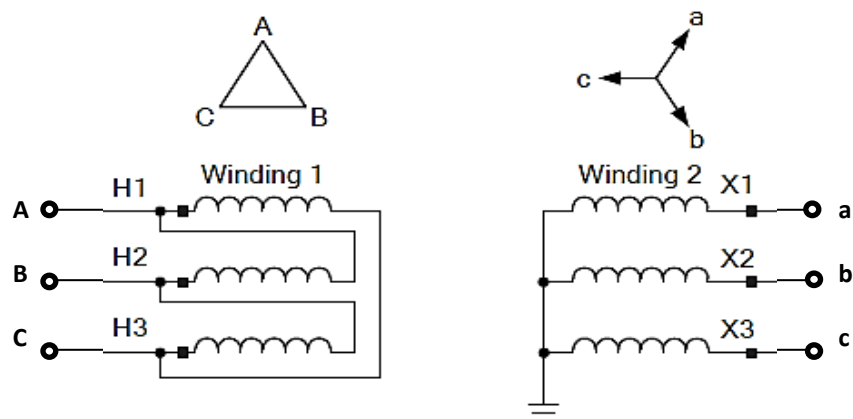


Figure 3: ANSI Standard Delta-Wye Transformer, ABC System Rotation, Connected to H1-H2-H3

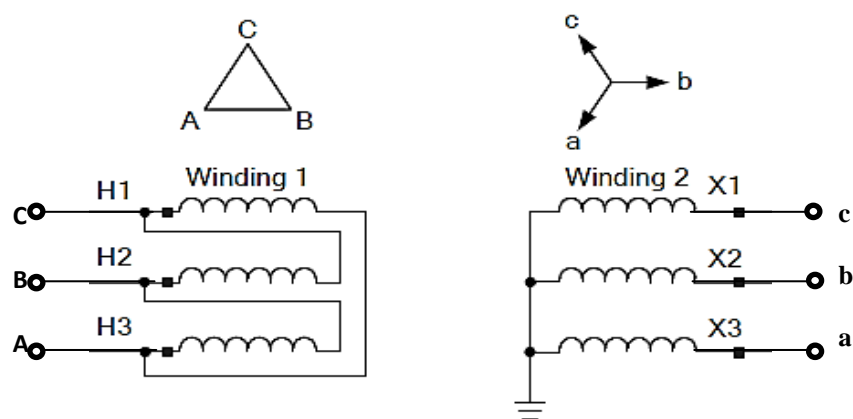


Figure 4: ANSI Standard Delta-Wye Transformer, ABC System Rotation, C-B-A Connected to H1-H2-H3

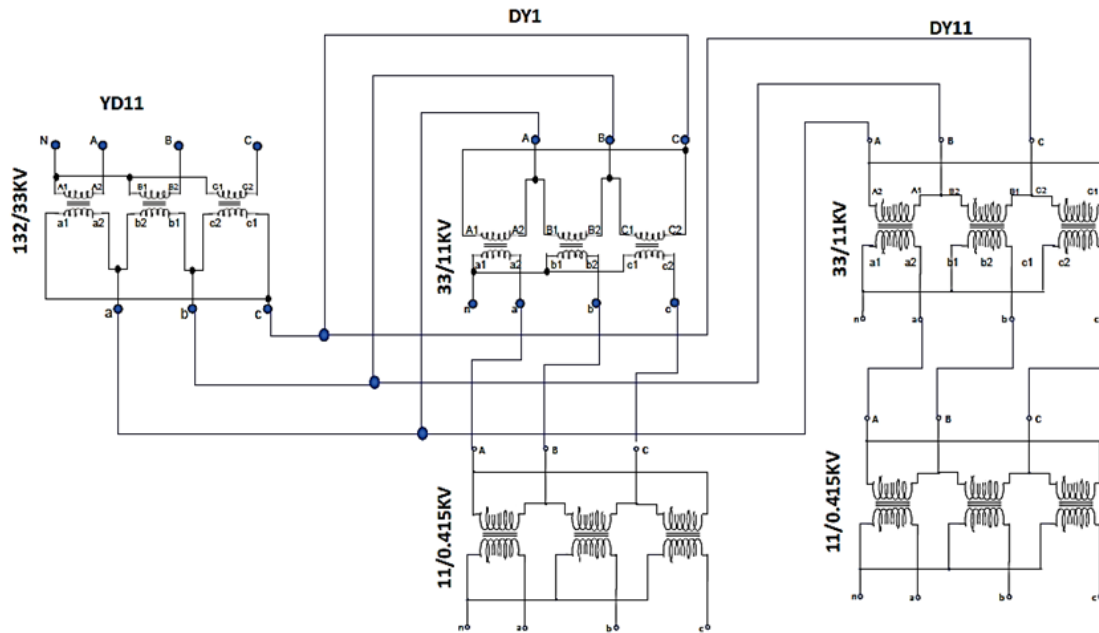


Figure 5: Comparison of Dy1 and Dy11 Vector-group Configuration connection on the 33/11kV Power System.

The first instance is the polarity convention shown in figure 3 In transformer phase rotation, connection of Polarity and Non-polarity winding terminals play very important roles in phase relationship and phase rotation. For the transformer nameplate drawing in Figure 3, if ABC phase rotation is assumed, the high-side currents will lead the associated low-side currents by 30 degrees. This is a DABY connection because the polarity of A-phase is connected to the non-polarity of B-phase.

The transformer nameplate shown in Figure 4 is exactly like the nameplate in figure 6, but now the system phase connections to the H1, H2, and H3 terminals have changed. Notice that A-phase is now connected to H3 and C-phase is now connected to H1. This is a DACY connection because the polarity of A-phase is connected to the non-polarity of C-phase.

The corresponding winding configurations are illustrated in figure 4 the corresponding phasor diagram of Dy11, 33/11kV Power transformer supplying Dy11, 11/0.415kV Distribution Transformer is also illustrated in figure 5

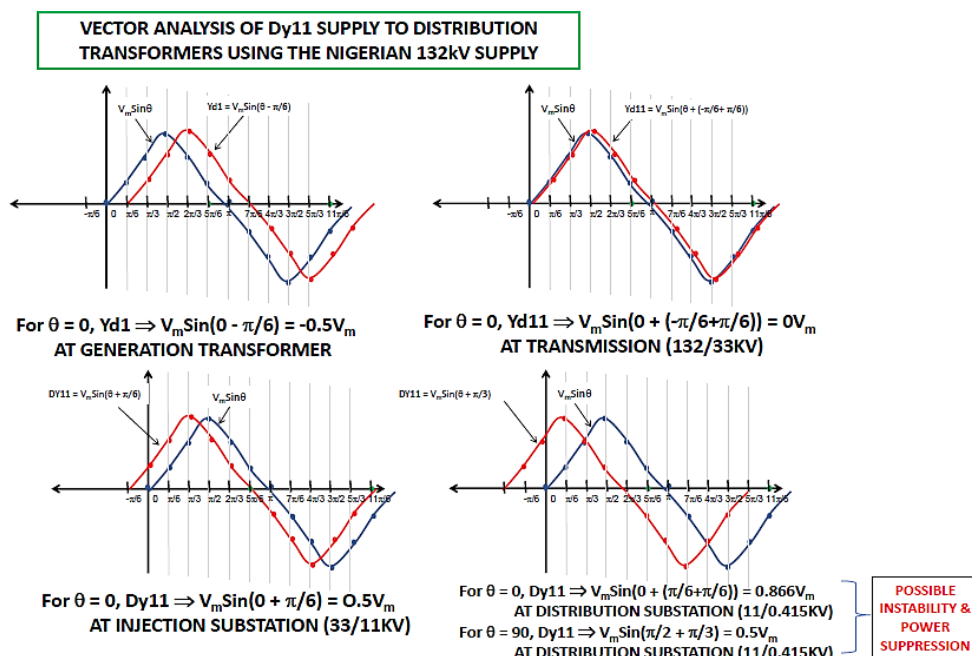


Figure 6: Voltage wave-form based on the Vector-group for Dy11 on the 33/11kV Power System

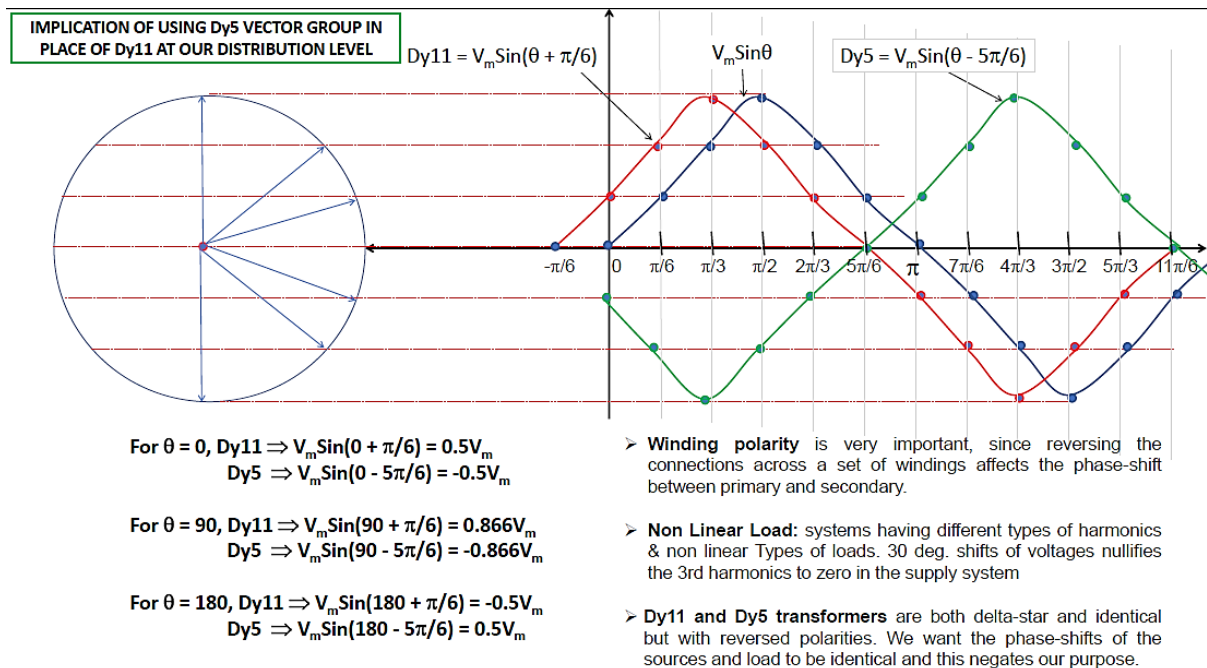
Any **phase angle difference** between the two waveforms is known as **phase shift** and causes an error when trying to determine the true power consumption. However, a **phase shift** of the current wave form from the input of a current **transformer** to the output is a common problem.

In terms of power flow, when metering or monitoring the amount of power dissipated in a circuit it is important to have an accurate measurement of each of the two contributing waveforms, voltage and current. Accuracy is not only necessary for amplitude of the two waveforms, but also the phase relationship between the waveforms must be considered. Any phase angle difference between the two waveforms is known as phase shift and causes an error when trying to determine the true power consumption. When metering or monitoring, the use of components that add minimal or at least predictable amounts to the phase shift are important to allow for accurate results.

#### 4.1 Replacement of Dy11 with Dy5

One of the common problems that confront our Distribution Network is the installation of Dy5 in place of Dy11. The phase Rotation diagram in figure 11 below gives the illustration of the implication.

With regards to theory, there are no special advantages of Dyn11 over Dyn5. In isolated applications there is no advantage or disadvantage by using Dy5 or Dy11. If however we wish to interconnect the secondary sides of different Dyn transformers or use them in redundancy to feed the same secondary loads, we must have compatible transformers.



**Figure 11: Phasor relationship between Dy11 and Dy5 with reference to Fundamental Phasor at source**

#### 4.2 Implications of the Vector Group Star-star 3-phase Yyn, 11/0.415KV Transformer connection

The Nigerian Electricity Management Services Agency (NEMSA) tried to evaluate the implication of this type of installation on our 33/11/0.415kV Distribution System. The first thing of note here is that the Primary winding has a “FLOATING NEUTRAL” not connected to earth. It was suspected that this situation could result to generation of Harmonics in the System particularly **unbalanced load or unsymmetrical fault conditions**.

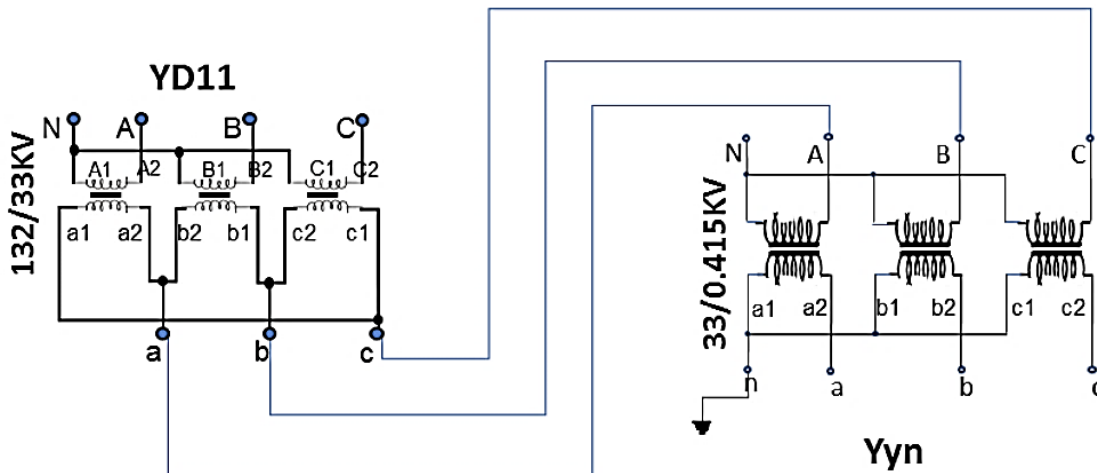


Figure 15: Connection Diagram for Yyn33/0.415kV Distribution Transformer on 132/33kV Network.

### V. Problem Analysis

It is a well-known fact that for standard power/distribution transformer with vector group Dy (i.e. Delta-star connection) the phase to ground fault on the LV side (i.e. star side) is manifested as phase-to-phase fault on the transformer HV side (i.e. delta side). Question can be raised how different type of faults will be seen across the power transformer with variable phase angle shift? Our case is shown in figure 7.

The knowledge of the fault current distribution is most important for transformer and **system backup protection** such as distance protection, over-current protection and earth-fault protection. Figure 7a is a typical connection diagram, and 7b is current distribution for single-phase to earth fault. The fault current distribution for phase-to-phase fault is also shown in figure 7c.

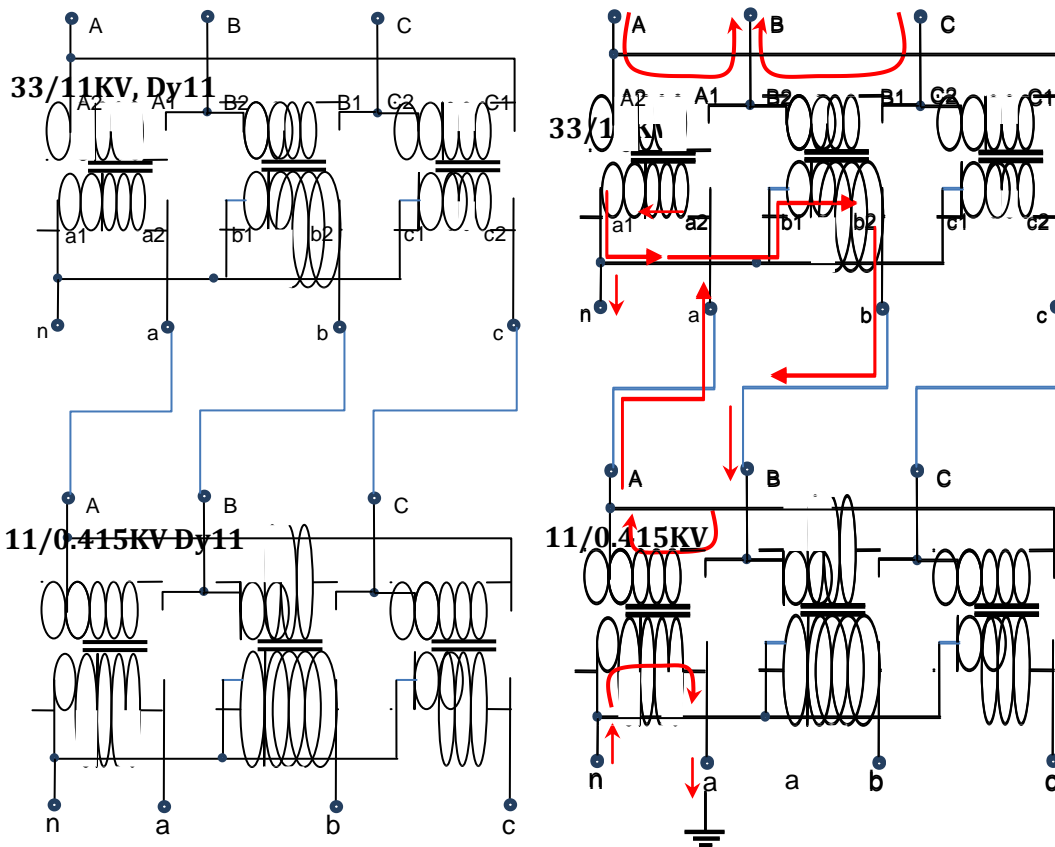


Figure 7a: Normal Dy1/Dy11 interconnection

Figure 7b: Single phase to ground current flow

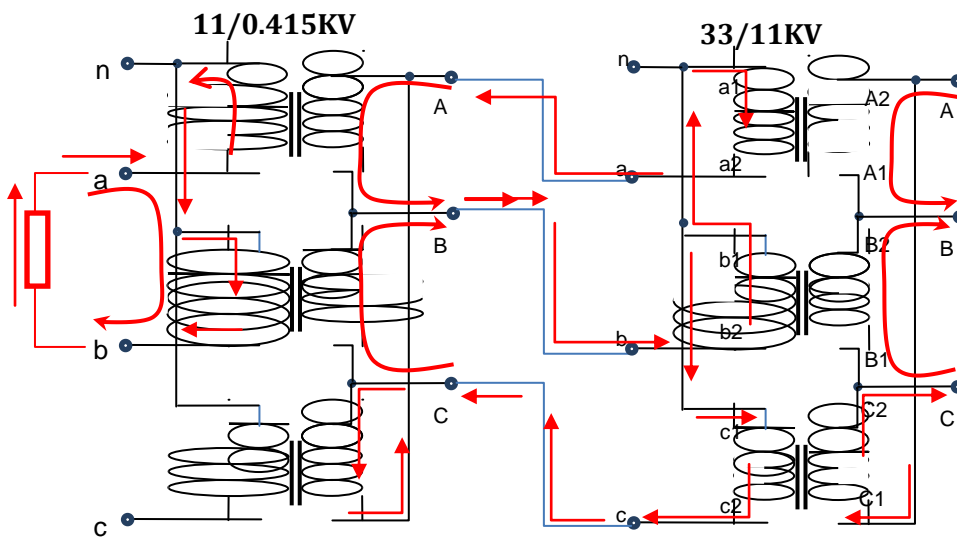


Figure 7c: Fault current flow with phase-to-phase fault

**Figure 7: Typical Current Distribution in Dyn11 Power & Distribution Transformers.**

It can be seen from figure 7b above that even though the line-to-line voltage ratio is N/1, the actual turns ratio is of the range given by<sup>6</sup>:

$$\frac{N}{(1/\sqrt{3})} = \frac{N\sqrt{3}}{1}$$

When a phase to earth/neutral fault occurs in low voltage side of the distribution transformer, the amount of the short circuit current is shown in the following formula:

$$\begin{aligned} I'_{SC\phi-N} &= \frac{E}{\frac{1}{3}(Z_1+Z_2+Z_0)N\sqrt{3}} \\ &= \frac{EN}{\frac{1}{3}(Z_1+Z_2+Z_0)N^2\sqrt{3}} \\ &= \frac{\frac{1}{\sqrt{3}} E'}{\frac{1}{3}(Z_1'+Z_2'+Z_0')} \end{aligned}$$

The equivalent short circuit current on the HV side of the transformer is given by:

$$I_{SC\phi-N} = \frac{E}{\frac{1}{3}(Z_1+Z_2+Z_0)}$$

It is clear from the above formula that for phase to earth fault, the fault current on the LV side must be multiplied by (1/√3) if we want to know the referred current on the HV side. This will circulate as phase-to-phase current on the HV and LV side of our Power Transformer.

### 5.1 Differential Current Considerations

**From differential current point of view**, we shall consider the classic and typical voltage and current definitions used for a three-phase, two-winding Power Transformer shown in figure 8, and also take our power transformer together with the downstream distribution transformer as a case of two-winding transformer with arbitrary phase angle shift  $\Theta$  (+60°).



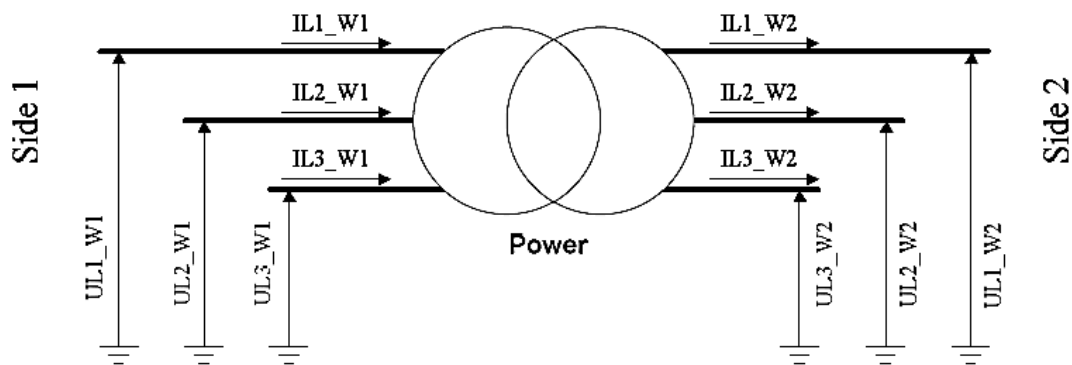


Figure 8: Typical voltage and current reference direction for a transformer<sup>10</sup>

The standard three-phase power transformers introduce a fixed phase angle shift  $\Theta$  of  $n \cdot 30^\circ$  ( $n=0, 1, 2, \dots, 11$ ) between its winding 1 and winding 2 side no-load voltages to achieve the standard  $30^\circ$  phase shift, as shown in Figure 9<sup>10</sup> below for the cascaded Dy11.

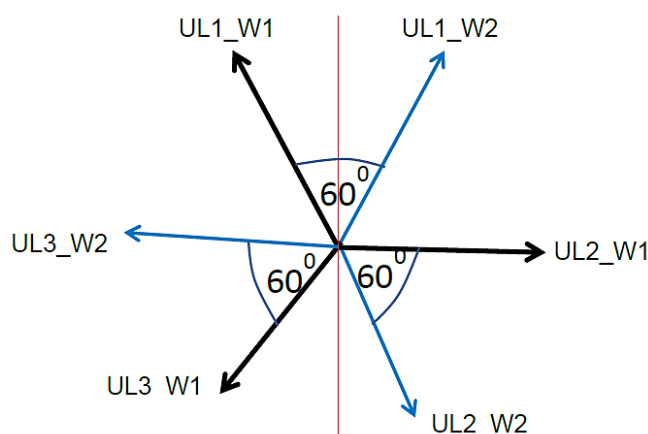


Figure 9: Phasor diagram for individual phase no-load voltages for our cascaded Dy11

If one now considers only the case of two-winding transformer with arbitrary phase angle shift  $\Theta$ , as shown in Figure 9 with additional assumption that during through-faults (i.e. external faults) all three differential currents will be zero in all phases, then the equation can be derived to calculate the S-side individual phase currents  $I_{S1}$ ,  $I_{S2}$  &  $I_{S3}$  from the L side phase currents  $I_{L1}$ ,  $I_{L2}$  &  $I_{L3}$  in primary amperes.<sup>1</sup>

In this consideration current magnitude diagrams shall be provided for  $-60^\circ < \Theta < 60^\circ$  which is the most commonly used range for the phase shift angle of special power transformers in practical installations.

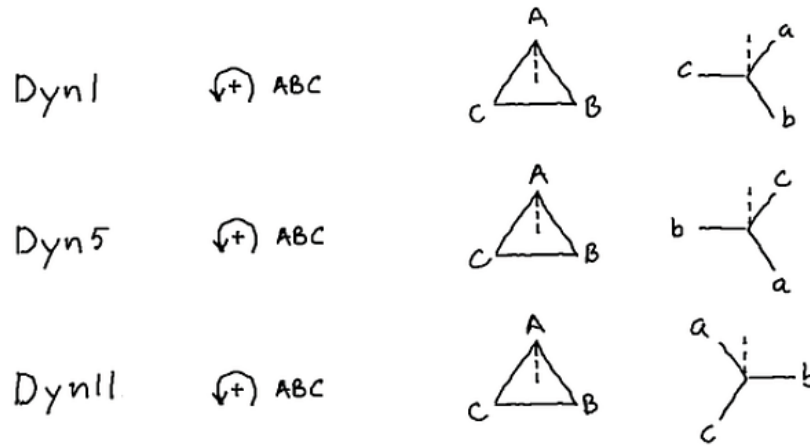
### 5.2 Unbalance System Considerations

There are possibilities of voltage and current unbalances that can possibly give rise to harmonics. Any deviation in voltage and current waveform from perfect sinusoidal, in terms of magnitude or phase shift is termed as unbalance.

In ideal conditions such as with only linear loads connected to the system, the phases of power supply are 120 degree apart in terms of phase angle and magnitude of their peaks should be same. On distribution level, the load imperfections cause current unbalance which travel to transformer and cause unbalance in the three-phase voltage. Even minor unbalance in the voltage at transformer level disturbs the current waveform significantly on all the loads connected to it. Not only in the distribution side but through the transformer, voltage unbalances disturb the high voltage power system as well.

### 5.3 Dy5 Transformers in the 11/0.415kV Network

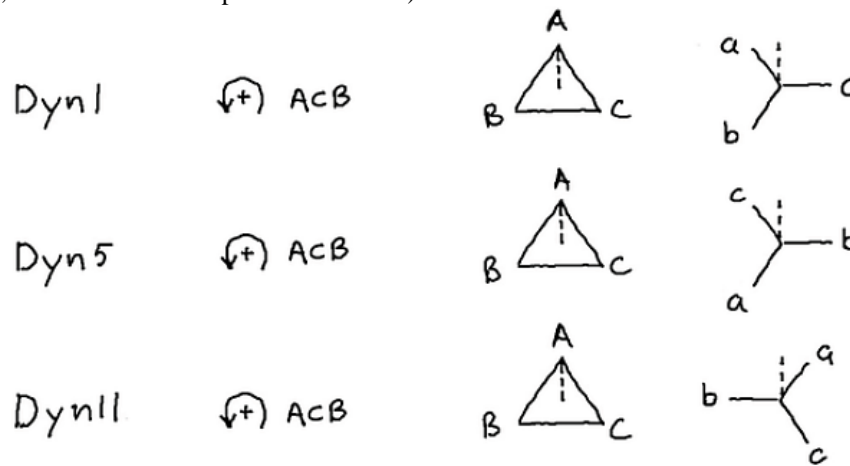
Let us take a look at the vector groups for a Dyn1, Dyn5 and Dyn11 when excited by counterclockwise, positive sequence, phase rotation ABC as shown in figure 10 below<sup>11</sup>.



**Figure 10: Phasor Diagrams of Positive Sequence Phase Rotation of Dy1, Dy5 and Dy11<sup>11</sup>**

Note that the vector groups for the Dyn1 and Dyn5 seem to be in phase with each other but the phase rotation of the bushings do not match, with the Dyn5 lagging the Dyn1 by  $120^{\circ}$ . Also note that the output vector group of a Dyn1 also lags a Dyn11 by  $60^{\circ}$ , and the difference in output between the Dyn11 and Dyn5 and is  $180^{\circ}$  degrees.

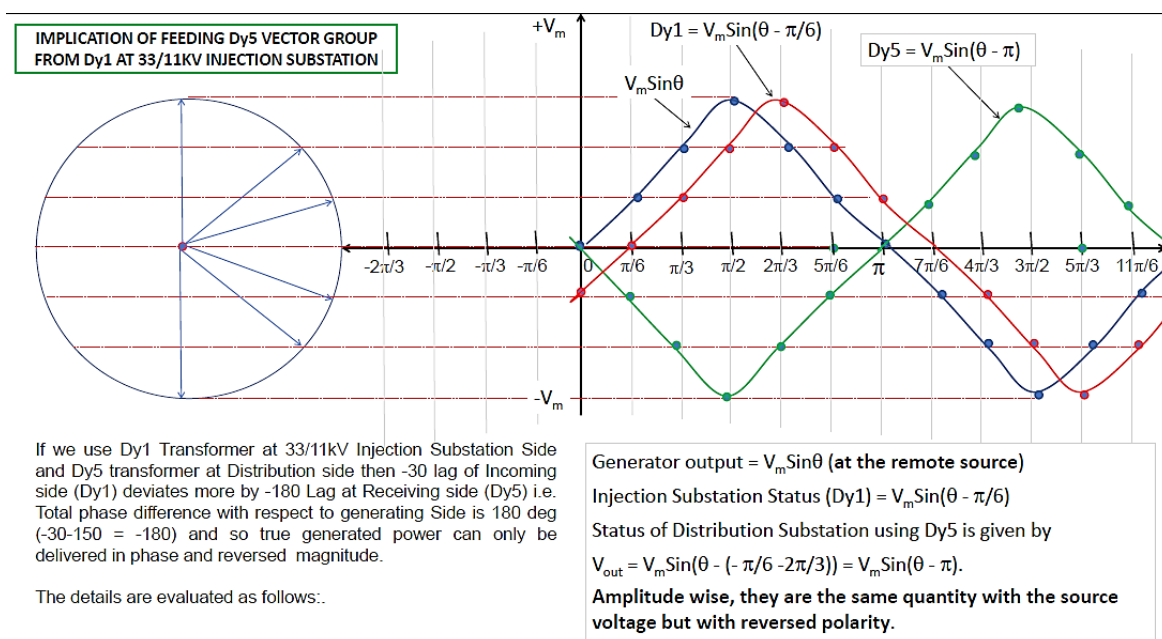
When the phase rotation of the excitation source is reversed from ABC to ACB, the vector groups are mirrored as shown in figure 11 below (a phase rotation meter connected ABC would rotate in the negative direction; or if connected ACB, would rotate in the positive direction):



**Figure 11: Phasor Diagrams of Counterclockwise Phase Rotation of the Vector Groups<sup>11</sup>**

So, there are the implications of matching the vector groups of a Dyn11 and Dyn5. Given a Dyn11 with positive sequence phase rotation ABC, a Dyn5 will have the same vector group if the phase sequence is reversed. **Correction can only be obtained when the HV and LV terminals are matched in certain configuration.** Phase sequence and phase rotation is critical to certain loads.

If we use Dy1 Transformer as the source to a Dy5 Distribution Transformer, then the  $-30^{\circ}$  lag of generating side (Dy1) is further lagged by  $-150^{\circ}$  Lag at Receiving side (Dy5) so Total phase difference respect to source is  $180^{\circ}$  deg ( $-30 + -150 = -180$ ). This is illustrated in figure 12 below:



**Figure 12: The implication of feeding a Dy5 transformer from a standard 33/11kV Dy1 Substation.**

The practical implication is that if we label the phases on HV clockwise as R- Y-B from left to right, then the LV side must be counterclockwise or Right to Left.

For a single transformer feeding an isolated load, this phase reversal will be of no consequence, long as the output voltages and phase sequences are correct. The problems arise if we are using two transformers to supply one load. For example, if two transformers are used to supply the same premises, one duty and one standby, with a manual or automatic changeover switch on the secondaries. If the switch is operated while both transformers are live, the load voltages will (almost) instantly reverse polarity. Some loads will not like this and may trip their protection. Another example is two identical transformers running in parallel. These must have the same vector grouping otherwise they will short circuit the input supply when the parallel connection is made.

By doing some unconventional connections externally on one side of the Transformer, an internal connected Dyn1 transformer can be changed either to a Dyn5(-150°) or Dyn9(+90°) connection. This will be discussed later.

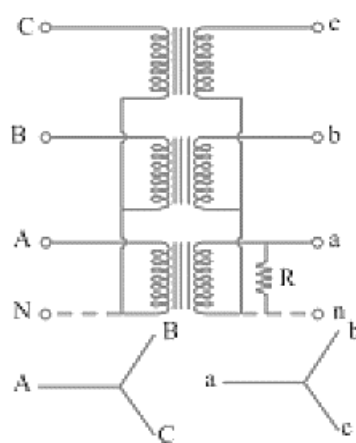
#### 5.4 The Yyn Transformer problem

The first consideration centred on a possible distortion in the Power Supply that can create problems for the source. **The Protection System cannot be guaranteed because of distortion in Phase-angles.**

The direct consequences of this are as follows:

- a. The effects of the harmonic currents are:
  1. Additional copper losses due to harmonic currents
  2. Increased core losses
  3. Increased electro-magnetic interference with communication circuits.
- b. On the other hand, the harmonic voltages of the transformer can cause:
  1. Increased dielectric stress on insulation
  2. Electrostatic interference with communication and other control circuits.
  3. **Resonance between winding reactance and feeder capacitance.**

Because of ungrounded neutral, and presence of third-harmonic voltages, if we place a single load between phase 'a', an unbalanced load to the neutral, the neutral point shifts thereby making the three line-to-neutral voltages unequal. Figure 13 illustrates a bank of three transformers connected in Y on both the primary and the secondary sides as shown.



0° Angular Displacement

**FIGURE 13: Illustration of effect of Unbalanced Loading**

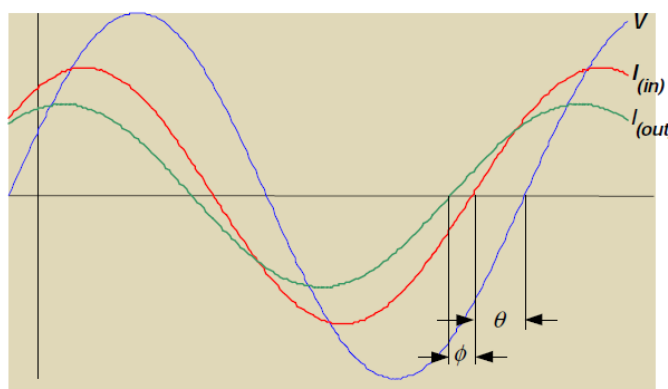
The effect of unbalanced loads can be illustrated by placing a single load between phase ‘a’ and the neutral on the secondary side. With **very low resistance approaching a short-circuit connected between point ‘a’ and the neutral**, only a very small amount of current will flow of reduction of voltage  $V_{an}$  due to neutral shift. Therefore, under short-circuit conditions, the neutral is shorted to phase ‘a’, reducing  $V_{an}$  but increases  $V_{bn}$  and  $V_{cn}$ , and line voltage on phase ‘A’ practically reduces to zero whereas  $E_{BN}$  and  $E_{CN}$  will rise to nearly full primary line voltage causing stress at the transformer neutral.

The consequences are as follows:

- i. Non-triplen harmonics like fundamental, become  $\sqrt{3}$  times phase value and appear in the line voltages.
- ii. Line currents remain sinusoidal except for non-triplen harmonic currents. Flux wave in each transformer will be flat topped and the phase voltages remain peaked.
- iii. The potential of the neutral is no longer steady. The star point oscillates due to the third harmonic voltages. This is termed as “oscillating neutral”.
- iv. Harmonics currents cause additional  $I^2R$  loss, core loss, magnetic interference with protective relays and interference in communication circuits.
- v. Harmonic voltages cause increased dielectric stress, interference with communication circuits and resonance between inductance of the transformer winding and the capacitance of the transmission line. Therefore, harmonics should be avoided.

## VI. CONSEQUENCES OF USING NON-STANDARD VECTOR GROUP

Because of inductive and capacitive loading, ac mains voltage and current are sometimes out of phase, so when a CT is used, the measured current has a phase lead (or lag) over the original current. This is illustrated in figure 14 below.<sup>13</sup>



**Figure 18: CT Phase Response<sup>13</sup>**

In Figure 14, the input mains current,  $I_{(in)}$ , leads the voltage,  $V$ , by  $\theta$  and the output current,  $I_{(out)}$  further leads  $I_{(in)}$  by  $\phi$ . The actual power is given as

$$P = V_o I_o \cos\theta \quad (1)$$

where  $V_O$  is the maximum ac input voltage,  $I_O$  is the maximum ac input current, and  $\cos\theta$  is the power factor.<sup>13</sup>

The measured power is represented as;

$$P = K_{(V)} V'_O K_{(I)} I'_O \cos(\theta + \phi) \quad (2)$$

where  $K_{(V)}$  is the scale-down factor for voltage ( $V_O = K_{(V)} V'_O$ ),  $K_{(I)}$  is the scale-down factor for current ( $I_O = K_{(I)} I'_O$ ), and  $\cos(\theta + \phi)$  is the measured power factor.<sup>13</sup>

The measured error is given by;

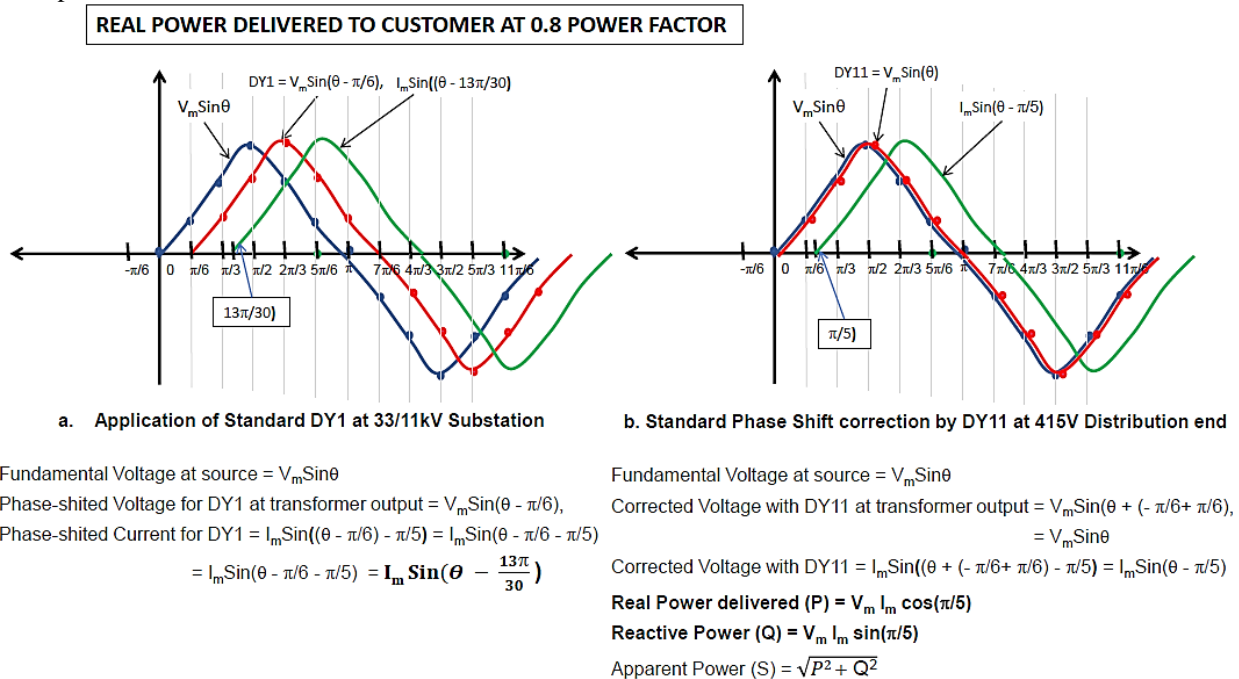
$$E_{(m)} = 1 - \frac{P'}{P} = 1 - \frac{\cos(\theta + \phi)}{\cos\theta} \quad (3)$$

The error is a nonlinear function of the power factor. As the power factor decreases, the error becomes significant. For example, with a power factor of 0.5 and a phase shift of  $1^\circ$ , the error is an unacceptable 3%.<sup>13</sup>

### 6.1 Power and Energy Requirements

It must be noted that at this utilisation output point, the output voltage is expected to be a replica of and in phase with the fundamental potential at the source of supply. If phase shift is sustained or expanded in the power transformer, it must translate to the current transformers providing the actual power and fault status of the system. Introducing current phase shift due to Power Factor, we have the diagram of figure 15.

It can be demonstrated that **Real Power consumption** become lesser than **Apparent Power** as Power Factor gets affected because, any shift in the current waveform from the voltage waveform creates a power factor lower than normal. **Power factor (PF) is the ratio between the true power (Watts) dissipated by the load and the apparent power (VoltAmps) that must be generated to satisfy the load.** Details are discussed in the technical implications section below.



**Figure 15: Sustenance of Phase shift due to Power Factor using Standard Vector Group**

For delta/star ( $\Delta/Y$ ), or star/delta ( $Y/\Delta$ ) transformer windings connections there is a phase shift in a balanced voltage and currents of typically  $\pm 30^\circ$  depending on transformer connections<sup>12</sup>. As presented in figure 2, with a transformer  $-30^\circ$  phase shift lagging (Dy1), a transformer with  $+30^\circ$  will return the waveform back to and in phase with the original generated value.

In the example shown in figure 15 above, if we take into consideration a three-phase 500KVA, 11/0.415kV Distribution Transformer, the rated current at the 415V end is given by:

$$I_O = \frac{500 \times 10^3}{\sqrt{3} \times 415} = 695.6A$$

Where  $I_0$  = Load Current.

It follows from figure 15 that Real Power delivered is given by;

$$P_O = I_0 V_0 \cos(\pi/5) = \sqrt{3} * 695.6 * 415 * \cos(36^\circ) = 404,508 \text{ KW}$$

$$\text{Reactive Power, } Q_O = I_0 V_0 \sin(\pi/5) = \sqrt{3} * 695.6 * 415 * \sin(36^\circ) = 293,892.6 \text{ KVAR}$$

$$\text{Therefore, Apparent Power, } S_O = \sqrt{P^2 + Q^2} = \sqrt{404.51^2 + 293.9^2} = 500 \text{ KVA}$$

In the case of using Dy11 Vector Group at the 33/11kV Injection Substation, the situation translate to the diagram of figure 16.

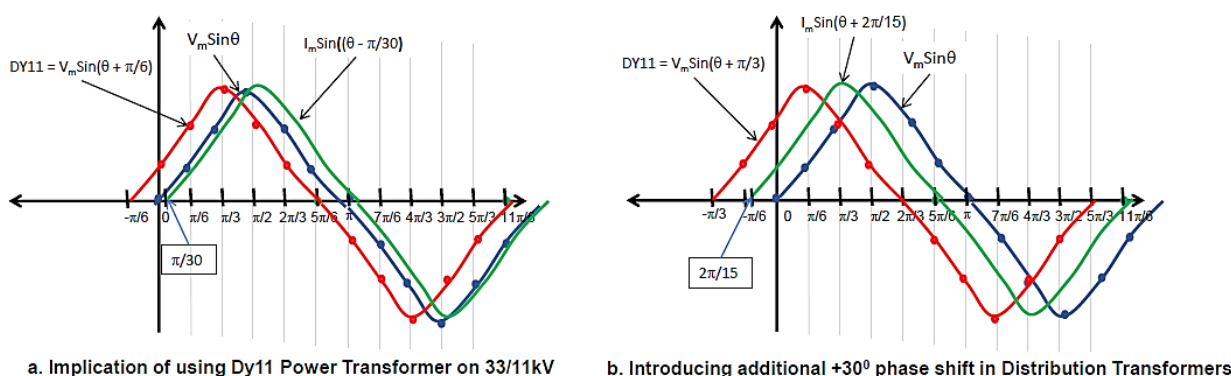
Again, if we take into consideration a three-phase 500KVA, 11/0.415kV Distribution Transformer, it follows from figure 15 that Real Power delivered is given by;

$$P_O = I_0 V_0 \cos(2\pi/15) = \sqrt{3} * 695.6 * 415 * \cos(24^\circ) = 456,772.73 \text{ KW}$$

$$\text{Reactive Power, } Q_O = I_0 V_0 \sin(2\pi/15) = \sqrt{3} * 695.6 * 415 * \sin(24^\circ) = 203,368.32 \text{ KVAR}$$

$$\text{Therefore, Apparent Power, } S_O = \sqrt{P^2 + Q^2} = \sqrt{456.8^2 + 203.4^2} = 500 \text{ KVA}$$

**REAL POWER DELIVERED TO CUSTOMER AT 0.8 POWER FACTOR AND 60° PHASE SHIFT**



Fundamental Voltage at source =  $V_m \sin \theta$   
 Phase-shifted Voltage for DY11 at transformer output =  $V_m \sin(\theta + \pi/6)$ ,  
 Phase-shifted Current for DY11 =  $I_m \sin((\theta + (\pi/6 - \pi/5)))$   
 $= I_m \sin(\theta - \pi/30)$

Fundamental Voltage at source =  $V_m \sin \theta$   
 Distorted Voltage with DY11 at transformer output =  $V_m \sin((\theta + (\pi/6 + \pi/6)))$   
 $= V_m \sin(\theta + \pi/3)$   
 Corrected Voltage with DY11 =  $I_m \sin(\theta + (\pi/3 - \pi/5)) = I_m \sin(\theta + 2\pi/15)$   
**Real Power delivered (P) =  $V_m I_m \cos(2\pi/15)$**   
**Reactive Power (Q) =  $V_m I_m \sin(2\pi/15)$**   
 Apparent Power (S) =  $\sqrt{P^2 + Q^2}$

**Figure 16: The illustration of delivering power using Dy11, 33/11kV Power Transformer.**

**The implication here is that sustaining the apparent power of 500 KVA requires that more active power be supplied to the tune of about 13%. That is, Real Power requirement will jump to 91% of apparent power as against 80% envisaged from the source.**

In terms of energy consumed within one month of an average of twenty-eight (28) active days and 672 active hours, the following calculations apply:

$$\text{Total Energy to be billed based on standard 0.8 Power Factor} = 404.51 * 672 = 271,830.72 \text{ kWhr}$$

$$\text{Total Energy released due to wrong Power Factor application} = 456.8 * 672 = 306,969.6 \text{ kWhr}$$

$$\text{Energy Deficit in one month} = 306,969.6 - 271,830.72 = 35,138.88 \text{ kWhr}$$

$$\text{This translates to } 12 * 35,138.88 = 421,666.56 \text{ kWhr per year.}$$

**It accounts for a loss of about one and half month of the year. It could be worse depending on power availability.**

**6.2 Measurement Errors in Current Transformers**

In a complex Phase angle errors, the current transformer introduces a phase shift (or time delay) in the AC current signal, relative to the actual current. This is commonly measured in degrees and varies from 0.2 degrees for highly accurate CTs to as high as 6 degrees. At and near unity power factor. **At lower power factors, such**

as 0.7 or below (especially below 0.5), even small phase angle errors can cause large errors in the measured power and energy.

In order to correctly apply protection, it is necessary to properly compensate for the phase shift, using current transformers which monitor current magnitudes and phase relationship on both sides. The delta/star winding current transformers need to be connected in a way to compensate for a) Current magnitude; b) Phase angle shift; and c) provide zero sequence current. This is to ensure that the phase shifts created in the currents of the power transformer are compensated by the CTs. **In metering and protection circuits where phase shifts deviate from original design concept, errors are introduced.**

In the case of a lagging current (inductive loads), the CT phase angle error (assuming it is greater than one degree) will make the power factor and real power values look higher than they actually are, especially for low power factors. The corrected values will show a lower power factor and lower real power.<sup>14</sup>

This relationship is evaluated as follows<sup>14</sup>:

$PF_R$	Reported (measured) power factor
$P_R$	Reported (measured) real power
$\theta_{CT}$	CT phase angle error (leading, degrees)
$S = \frac{P_R}{PF_R}$	Apparent power (not affected by CT phase angle errors)
$\theta_R = \arccos(PF_R)$	Phase angle between line voltage and current (lagging, degrees), based on reported PF
$\theta_C = \theta_R + \theta_{CT}$	Phase angle between line voltage and current with the CT phase error (lagging, degrees).
$PF_C = \cos(\theta_C)$	Corrected power factor
$P_C = PF_C \cdot S$	Corrected real power
$Err\% = 100 \cdot \left( \frac{PF_R}{PF_C} - 1 \right)$	Percentage error in reported power

**The particular case of the power factors calculated above will be used as an example and proof of errors for the CTs in the 33/11kV Injection Substation.**

From figure 20, section... we proceed as follow assuming CT Phase Angle Error of 2°:

Assumed Power Factor between line voltage and current,  $PF_R = 0.81$  (lagging)

Assumed Real Power,  $P_R = 404.51$  KW

CT Phase Angle Error,  $\theta_{CT} = 2^\circ$  (leading)

Apparent power,  $S = P_R / PF_R = 404.51 / 0.81 = 499.4$  KVA  $\cong 500$  KVA

Phase angle between line voltage and current,  $\theta_R = \cos^{-1}(0.81) = 36^\circ$  (lagging)

Phase angle between line voltage and current with the CT phase error, is given by;

$$\theta_C = \theta_R + \theta_{CT} = (36 + 2) = 38^\circ \text{ (lagging)}$$

Corrected power factor with reference to Dy11 Power Transformer,  $PF_{CT} = \cos(38) = 0.788$

Actual Phase angle between line voltage and current,  $\theta_{RA} = 60^\circ - 36^\circ = 24^\circ$  (with additional Dy11 transformer and 60° phase shift).

Phase Angle with CT Error,  $\theta_C = (24 + 2) = 26^\circ$

Corrected power factor with reference to Power System Source,  $PF_{CS} = \cos(26) = 0.899$

Corrected Real Power,  $PF_C = S * PF_{CS} = 500 * 0.899 = 449.4KVA$

$$\%Error = 100 * \left( \frac{PF_R}{PF_{CS}} - 1 \right) = \left( \frac{0.81}{0.9} - 1 \right) * 100 = 10\%$$

This means that measurements from CTs located in this place will always have 10% Reading Error. By implication, for a customer using 600,000Kwhr per month consumption per month for instance:

Table 1: Calculations for Phase Angle Shift and Power Factor with CT Phase Angle Error

Current Phase Angle Shift, $\Theta_R$ (degree)	Assumed Power Factor	CT Phase Angle, $\Theta_{CT}$ (degree)	Apparent Power (S), KVA	Active Power Assumed (P), KW	Total Phase Angle with CT Error, $\Theta_C$	Actual Power Factor	Actual Active Power	% Error in CT Measurement
0	0.81	2	500	405	2	0.9994	499.70	-18.95
10	0.81	2	500	405	12	0.9781	489.07	-17.19
20	0.81	2	500	405	22	0.9272	463.59	-12.64
30	0.81	2	500	405	32	0.8480	424.02	-4.49
40	0.81	2	500	405	42	0.7431	371.57	9.00
50	0.81	2	500	405	52	0.6157	307.83	31.57
60	0.81	2	500	405	62	0.4695	234.74	72.53
70	0.81	2	500	405	72	0.3090	154.51	162.12
80	0.81	2	500	405	82	0.1392	69.59	482.01
90	0.81	2	500	405	92	-0.0349	-17.45	-2420.95
100	0.81	2	500	405	102	-0.2079	-103.96	-489.59
110	0.81	2	500	405	112	-0.3746	-187.30	-316.23
120	0.81	2	500	405	122	-0.5299	-264.96	-252.85
130	0.81	2	500	405	132	-0.6691	-334.57	-221.05
140	0.81	2	500	405	142	-0.7880	-394.01	-202.79
150	0.81	2	500	405	152	-0.8829	-441.47	-191.74
160	0.81	2	500	405	162	-0.9511	-475.53	-185.17
170	0.81	2	500	405	172	-0.9903	-495.13	-181.80
180	0.81	2	500	405	182	-0.9994	-499.70	-181.05

Assumed Apparent Power,  $S_A = 600,000 / 0.81 = 740,740.74VA$  (actual VA supplied)

Measured Apparent Power,  $S_M = 600,000 / 0.899 = 666,666.67VA$  = (measured VA)

**This is a deficit of -74,740.074VA or 74.74KVA to the power supply authority in a month for a single customer** and it is to the advantage of the customer.

Useful work is accomplished by **active power** while **reactive power** improves voltage stability and avoids voltage collapse. By implication, transformer active power utilisation is ensured at the expense of System Voltage Stability and this may lead to eventual System Voltage Collapse.

Table 1 below shows variation of Real Power and Power Factor with various Phase Angle shifts up to 180°.

It is interesting to know that at maximum power factor with error of 18.95% in CT, we can take up to 499.70KW, close to 100% apparent power after 60° phase shift we can barely up 50% and after 90° power is returned back to the system.

Figure 17 below shows the effect of Phase Shift on System Power Factor.



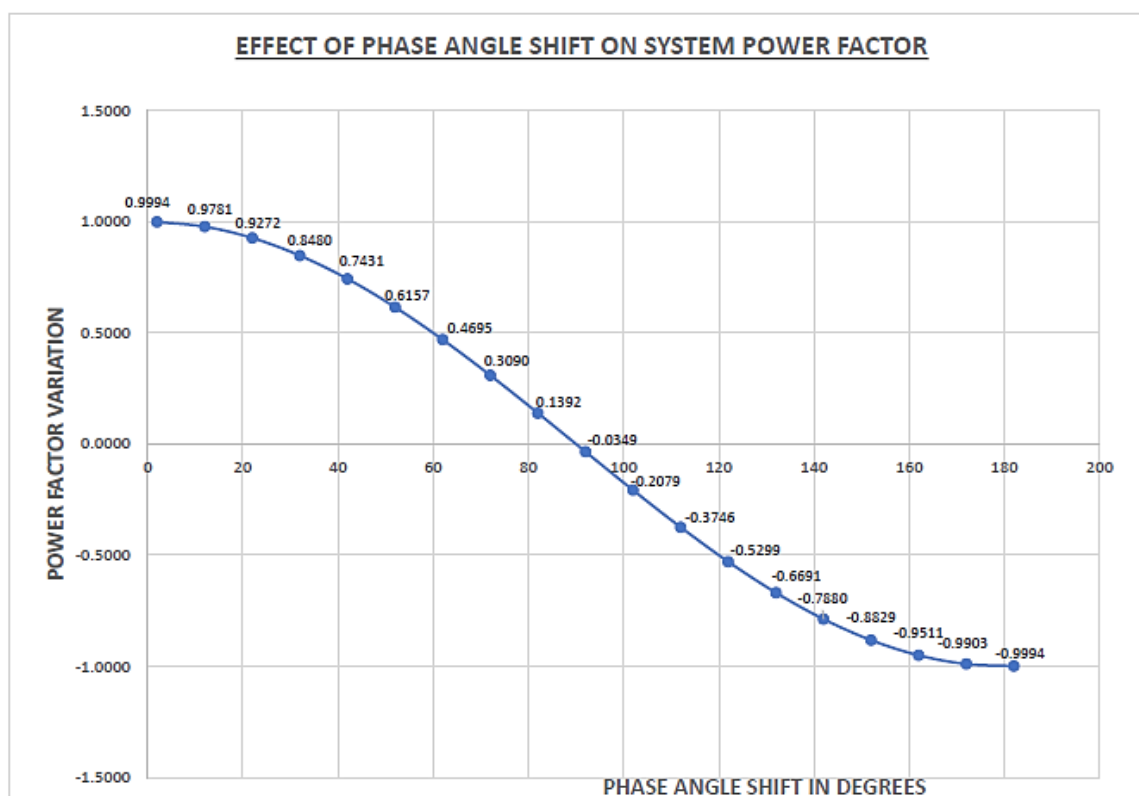


Figure 17: The effect of Phase Angle Shift on Power Factor.

As can be seen from the chart of figure 17:

- At minimum phase-shift, the power factor tends to unity and the real power consumption tends to apparent power supplied.
- At 30° phase-shift, the real power dissipated is about 0.866 x apparent power supplied and with 2° CT phase shift it is 0.8480 x apparent power.
- At 60° phase shift, real power dissipated tends to half of apparent power (about 0.5 x apparent power supplied)
- As the phase-shift tends towards maximum of 90° the real power consumption becomes invisible and apparent power becomes more reactive.
- Beyond 90° the power factor becomes negative and power is returned back into the system, the magnitude of which is dependent on phase angle shift.

Negative Power Factor produces reverse power flow in the system. A **negative power factor** occurs when the device (which is normally the load) generates **power**, which then flows back towards the source, which is normally considered the generator. This can be harmful for the surrounding circuit and the load because in reality, the net power is still outward because of the resistive part of the load that normally predominates. A transformer that produces negative power factor can be considered as simple generator without regulator and the negative power factor will cause the terminal voltage to rise above its open circuit value possibly causing damage to any voltage sensitive load. **It therefore follows that Dy5 fed from Dy1 Power Transformer has the tendency of reversing power flow except used in industries with sufficient machines to absorb the reactive power flow.** The effect of an isolated case may not be readily felt on an infinite bus system, but if this trend is allowed unabated and significant numbers are installed, it may spell doom for the power system.

Figure 18 is a chart of Power Factor versus Percentage error due to phase shift.

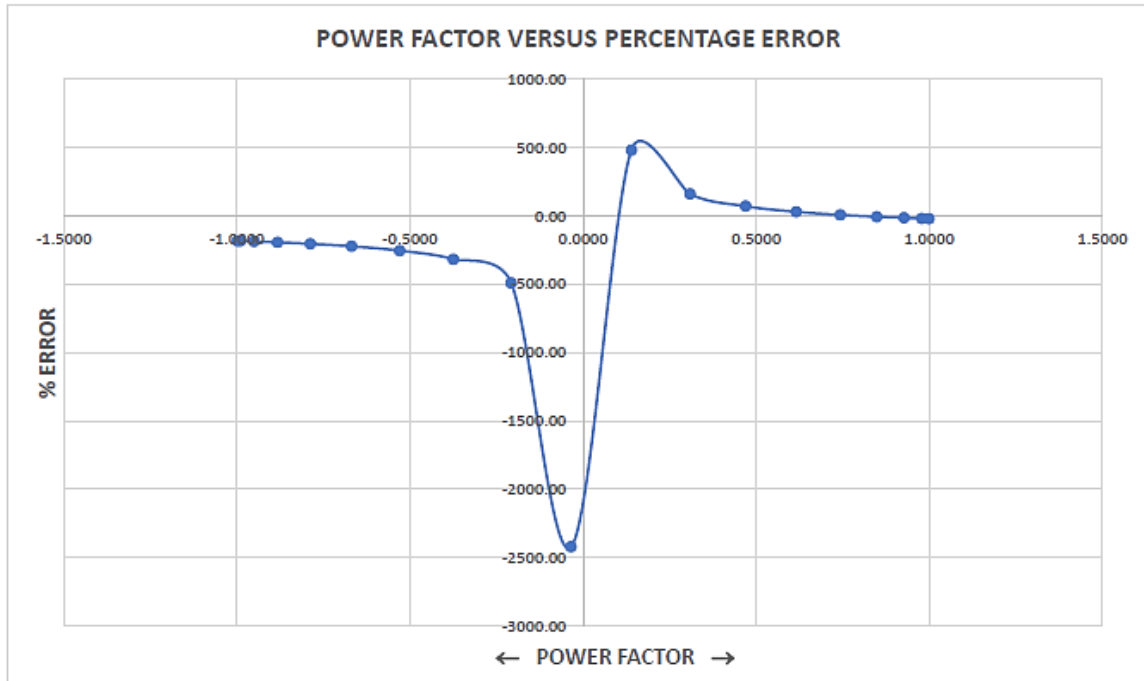


Figure 18: Curve of Percentage Error due to Phase Shift.

It will be noted from figure 18 that the peak of the error occurs at 90° translating to negative power factor afterwards with extremely high error. The adverse effect of negative power factor has earlier been discussed.

### VII. SUGGESTIONS ON TECHNICAL SOLUTIONS

There are valid technical approaches to overcome these problems, and these are categorised as follows:

1. Simple application of electrical machine phase rotation philosophy for the Dy1, Dy11.
2. Unconventional Phase Rotation Connections to convert Dy5 to Dy11.
3. Installation of Dyn1 Isolation Transformer to provide operational basis for connection of the Yy0 transformer to existing Yd11 at 132/33kV network.

#### 7.1 Application of Phase Rotation Techniques (Dy11 to Dy1)

In transformer phase rotation, connection of Polarity and Non-polarity winding terminals play very important roles in phase relationship and phase rotation.

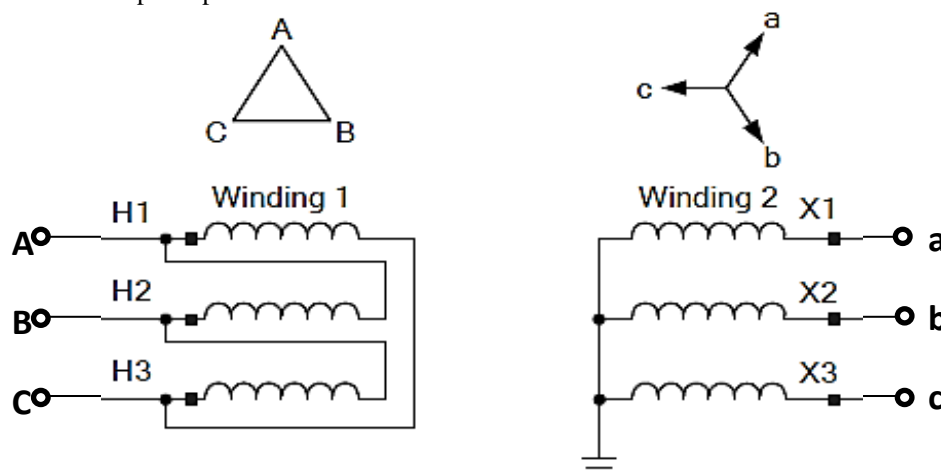


Figure 19: ANSI Standard Delta-Wye Transformer, ABC System Rotation, A-B-C Connected to H1-H2-H3

For the transformer nameplate drawing in Figure 19, if ABC phase rotation is assumed, the high-side currents will lead the associated low-side currents by 30 degrees. This is a DABY connection because the polarity of A-phase is connected to the non-polarity of B-phase.

The transformer nameplate shown in Figure 20 is exactly like the nameplate in figure 19, but now the system phase connections to the H1, H2, and H3 terminals have changed. Notice that A-phase is now connected to H3 and C-phase is now connected to H1. This is a DACY connection because the polarity of A-phase is connected to the non-polarity of C-phase.

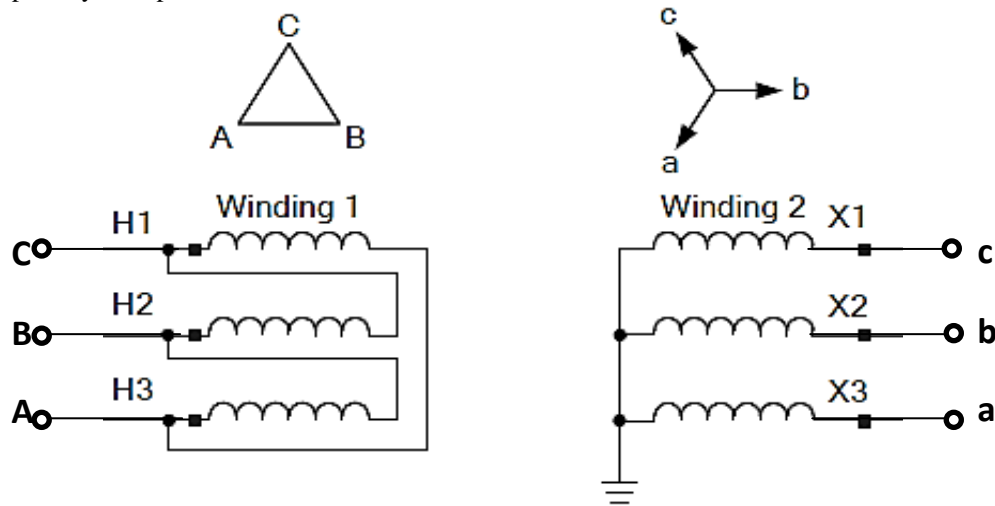


Figure 20: ANSI Standard Delta-Wye Transformer, ABC System Rotation, C-B-A Connected to H1-H2-H3

It is therefore clear from the above configuration analogy that we can provide the needed phase-shift compensation by re-configuring our Dy11 terminals from DACY configuration to DABY for equivalent Dy1 as in figure 21 below:

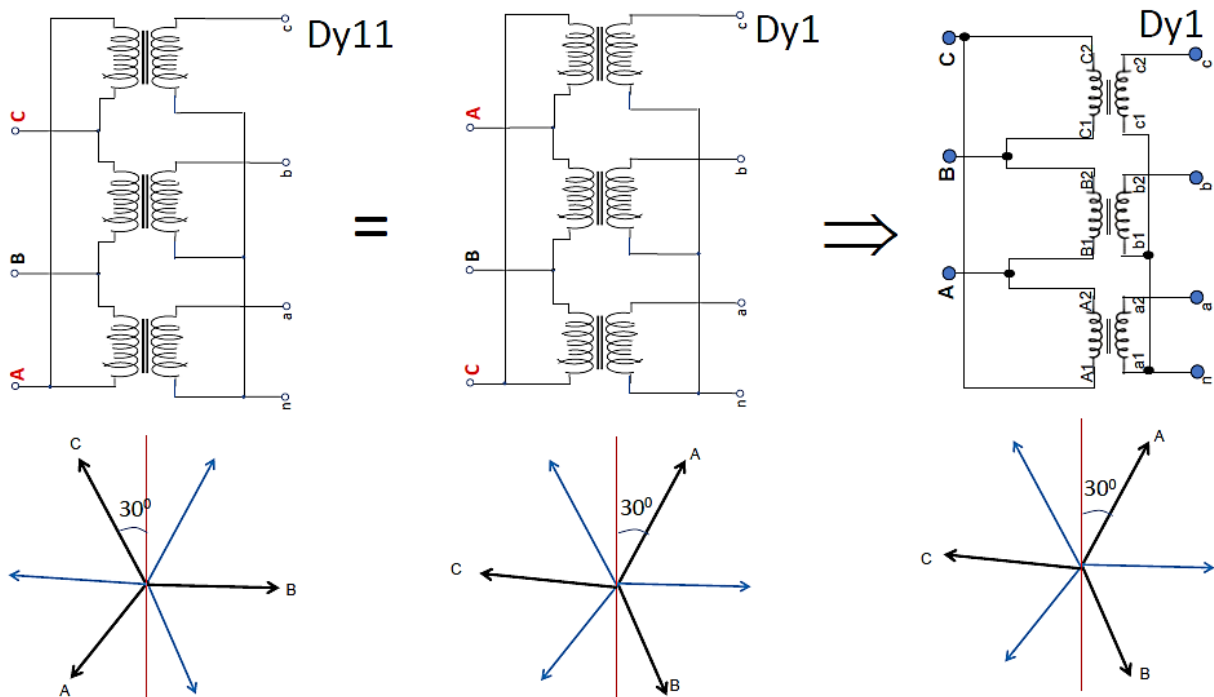


Figure 21: Technical transformation of Dy11 to Dy1 using Transformer Phase Relationship

7.2 External Unconventional Phase Connections to convert Dy5 to Dy11.

When these two sets of vector groups are compared, it becomes apparent that a Dyn11 vector group can be matched to a Dyn5 provided one of them has reverse phase rotation. There are two possible combinations. Given a Dyn11 with positive sequence phase rotation ABC, a Dyn5 will have the same vector group if the phase sequence is rotated:

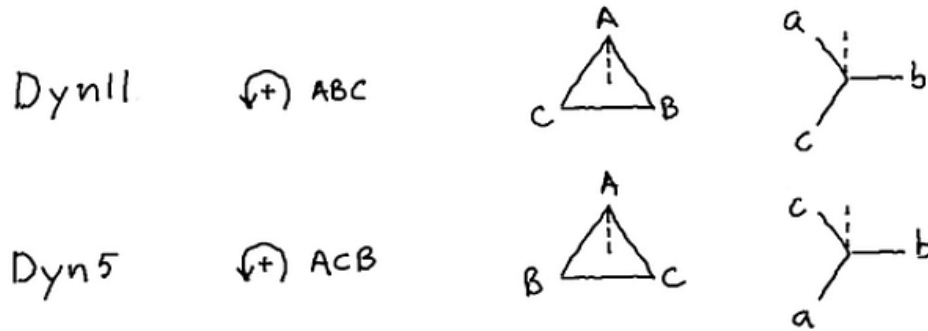


Figure 22: Phasor Diagrams showing comparison between rotated Dy11 and Dy5<sup>11</sup>

7.3 Dy5 Suggestions for the Yy0 Transformer neutral problem

1. Outright replacement was recommended to avoid technical complications.
2. If the financial burden is substantial and we still want to maintain the perceived advantages of single-phase loads provided by this transformer, it can only be tied into the system via a ratio 1:1, **Dyn1 Isolation Transformer** as illustrated in figure 23 below:

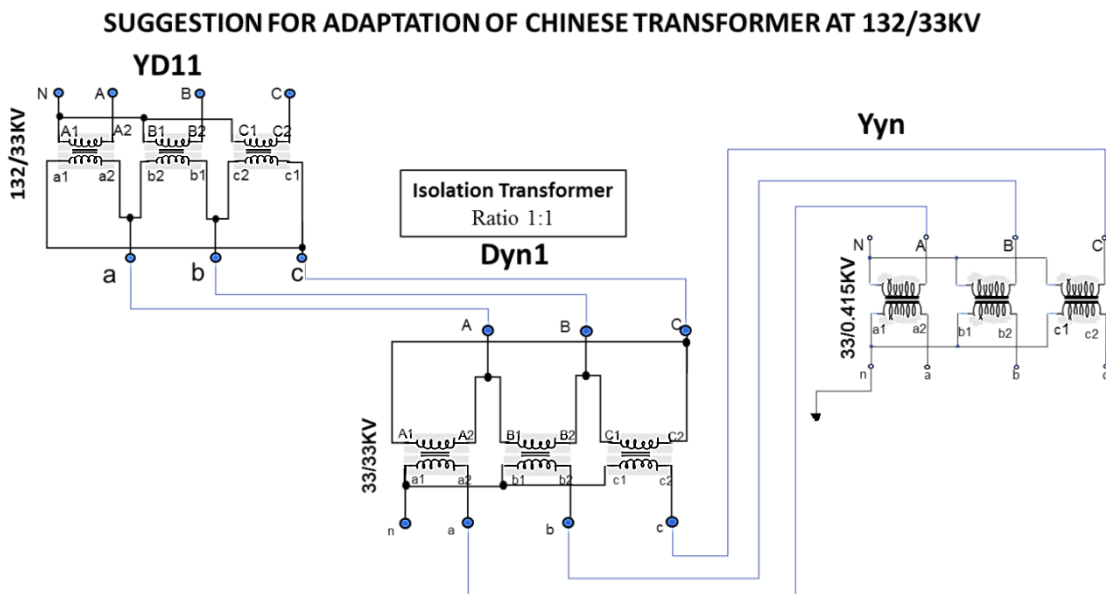


Figure 23: Application of Isolation transformer for connection of Yy0 Vector Group

The Isolation should be rated at least 1.25xFull-load Power to sufficiently account for the losses. Therefore, for 1500kVA, 33/0.415kV Yyn transformer, a 2000kVA, 33/33kV Dyn1 transformer is recommended.

VIII. CONCLUSION

Based on the foregoing evaluations and analysis, it can be safely concluded that there are implications in wrong installations of the vector groups Dyn11, Dyn5 and ungrounded Yyn0 in the Nigerian Electricity Distribution System. These implications include:

- a. Unwanted Circulating Currents in the system and Out-of-step voltages could adversely affect system operation and stability.
- b. Introduction of abnormal phase angle displacement that could cause problem to the entire Power System where additional 60° phase-shift has been introduced.
- c. Accuracy of Metering or Monitoring the amount of Energy in the circuit in leading to substantial energy deficit.
- d. Unbalance System Conditions involving possibilities of voltage and current unbalances that can possibly give rise to harmonics.
- e. Incompatibility of Dyn5 and Dyn11 in phase but reversed polarity can result to the load voltages will (almost) instantly reversing polarity causing damages, if we are using two transformers to supply one load in active redundancy.

- f. Floating or oscillating neutral from a non-standard vector group resulting in a possible distortion in the Power Supply such as harmonic currents and voltages that can create problems for the system.

**As a result of these development, it is concluded that unconventional Vector Group should be disallowed in the Nigerian National Grid, and where they already exist, suggested correctional principles be applied.**

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