

## Numerical Investigation of RC Exterior Beam Column Connections under Monotonic Loads

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**Abstract:** A finite element model of reinforced concrete beam column connections (BCC) using ABAQUS program is presented. The concrete is discretised into 4-node shell elements. Truss elements discretely model each single reinforcement bar. They are coupled to the concrete elements using the embedded modeling technique. The concrete damage plasticity model of ABAQUS is used to describe the nonlinear material behavior of concrete and steel plates of supports under monotonic loading. The parametric model is verified to experimental results taken from the literature. Eleven specimens were investigated in the experiment. Two specimens only were modeled. The effect of new parametric study was studied by ABAQUS. Change of column width, axial column load and concrete compressive strength were presented. It was found a close agreement between numerical and experimental results. Also, the column load has minor effect on the deformation of specimens. On other hand, as the column width and/or concrete compressive strength increased, the BCC capacity increased.

**Keywords:** Reinforced concrete beam column connections, shear joint failure, embedded modeling, ABAQUS, monotonic loading, column width, FEA, axial column load.

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### I. Introduction

The beam column connections (BCC) are one of important structural elements in concrete structures. This is due to its construction difficulty and its manual design. In several structural collapses, the BCC was the main reason particularly, when the building subjected to earthquake. Researchers have observed four types of failures that can take place in BCC [(Kiran and Genesio, 2014)]. These modes of failure can be classified as: - shear failure in the joint, slippage of the beam main reinforcement bars, yielding of the beam main reinforcement (beam hinging) and yielding of the column longitudinal bars (column hinging). Shear failure of BCC was the main cause in failure of several moment-resisting frame structures during recent earthquakes (Park and Mosalam, 2012).

The effect of axial load ratio on seismic behavior of interior beam-column joints was studied by FU et al. (2000). The data of interior RC beam-column sub-assembly was investigated by Murakami et al. (2000). These specimens failed in joint shear. The parameters affecting on joint shear capacity were studied in addition to a shear equation was induced. Several researchers have simulated the behavior of the BCC using finite element analysis software such as ABAQUS, ANSYS and VECTOR2. A cyclic tests on hybrid fibre concrete structural walls were proposed using ABAQUS and reported by Davide et al (2006). The effect of CFRP on RC beams behavior using ABAQUS was proposed by Yamane et al (2010). ABAQUS/Explicit (ABAQUS, version 6.12.3, 2012) was used to simulation of the current study.

In the present study, the finite element analysis (FEA) was used to model the behaviour of beam column connections. For validation, the study was carried out on two specimens of BCC that had been experimentally tested and reported by Mohamed et al. (2014). A parametric study including axial column load, column width and concrete compressive strength was induced.

### II. Research Significance

The FEA using ABAQUS facilitates the design and analysis of RC beam column connections for researchers and designers. Through FEA, the compressive strength of concrete, the failure mode of joint, the crack pattern, effect of column width and effect of axial column load ratio can be obtained. Therefore, with the proposed FEA, it was possible for engineers to achieve a reasonable solution for BCC behaviour.

### III. Experimental Results Considered

Experimental data was obtained from previous work by Mohamed et al. (2014). The research tested eleven RC exterior beam-column connections. This experimental program was tested under monotonic loading. All specimens had the same concrete dimensions. Each specimen had a cantilever beam of 900 mm length. The

high tensile steel (yield strength ( $f_y$ )= 400 MPa) was used for the top and bottom longitudinal bars of the beam and used for the main longitudinal steel reinforcement of the column. The used stirrups for both beam and column were made from normal mild steel bars (yield strength ( $f_y$ )= 250 MPa). The diameter was 8 mm and the spacing between stirrups of column was 150mm and it was 100mm for the beam. The specimen Jo contained three stirrups of 8mm diameter at joint panel. For all specimens, the compressive strength of concrete ( $f_{cu}$ ) was 25 MPa and young's modulus of steel was 200 kN/mm<sup>2</sup>. The ultimate tensile strength of concrete was taken according to Egyptian code (2012)  $0.6 \sqrt{f_{cu}}$  N/mm<sup>2</sup> because it did not mentioned in experiment. Figure.1 shows the concrete dimensions and reinforcement detailing for the base control specimen. The loading direction on the beam end was acted at the lower side. A vertical load of 200 kN was applied at the upper end of column for all specimens.

The experimental program was consisted of three groups plus the base control specimen (Jo). The first group included three specimens: J10, J11, and J12. This group studied the absence of the shear reinforcement at the beam-column connection. The specimen J10, which considered in the current study, was without stirrups at joint panel. Specimens of both second group and third group were not represented in the current study. Only two specimens Jo and J10 were investigated. Verification of experimental results using ABAQUS was obtained firstly then the parametric study was developed.

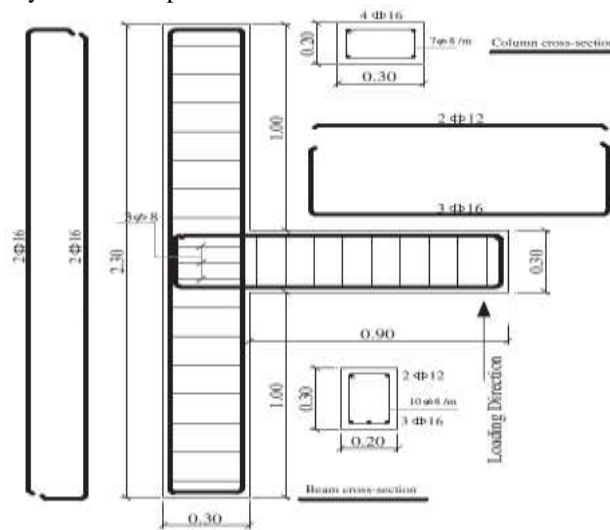


Figure.1 Concrete dimensions and reinforcement details for the base control specimen, J0 (Mohamed et al. (2014))

#### IV. Finite Element Analysis (FEA)

Finite element analysis was proposed to model the 2D nonlinear behaviour of the beam column connections. The Abaqus/standard (ABAQUS, version 6.12.3, 2012) was used for the analysis.

##### 4.1. Modeling of Material Properties

###### 4.1.1 Concrete

The concrete behavior was modeled by a plastic damage model. a two failure modes, tensile cracking and compressive crushing, were assumed in this model. The concrete damaged plasticity model in ABAQUS version 6.12.3 was used to simulate the concrete behavior for both the column and beam. The 2-D planar shell used for modeling of the RC beam column connection (BCC). The concrete behavior will be considered dependent on the embedded steel. The bond skid is modeled by embedded region. The boundary condition of the lower end and upper end of the column was simulated as hinged support and roller support respectively. The roller support was allowed the vertical movement when the axial column load applied. A vertical pressure load was applied on column to simulate the vertical load applied on column. A displacement of 40 mm was applied on free end of beam up word to simulate the applied load in test at same point.

The compressive strength,  $f_{cu}$ , was in the experimental work measured to be 25 MPa. Modulus of elasticity of concrete ( $E_c$ ) and concrete tensile strength ( $f_{ctr}$ ) were calculated by Egyptian code (2012) in equation (1) and equation (2) respectively:

$$E_c = 4400 \sqrt{f_{cu}} = 22000 \text{ MPa} \quad (1)$$

$$f_{ctr} = 0.6 \sqrt{f_{cu}} = 3 \text{ MPa} \quad (2)$$

Where  $f_{cu}$ , is given in MPa.

The stress–strain equations (3 and 4) proposed by Saenz (1964) was used to draw the compressive stress–strain curve for concrete:

$$\sigma_c = \frac{E_c \varepsilon_c}{1 + (R + R_E - 2) \left(\frac{\varepsilon_c}{\varepsilon_0}\right) - (2R - 1) \left(\frac{\varepsilon_c}{\varepsilon_0}\right)^2 + R \left(\frac{\varepsilon_c}{\varepsilon_0}\right)^3} \quad (3)$$

Where  $R = \frac{R_E (R_\sigma - 1)}{(R_E - 1)^2} - \frac{1}{R_E}$ ,  $R_E = \frac{E_c}{E_0}$  and  $E_0 = \frac{f_{cu}}{\varepsilon_0}$  (4)

and,  $\varepsilon_0 = 0.0025$ ,  $R_E = 4$ ,  $R_\sigma = 4$  as reported by Hu (1989). The stress–strain curve in compression for concrete is shown in Figure.2. Poisson’s ratio of concrete was taken 0.2. Same method was used to draw stress-strain curve of concrete when compressive strength equal 35 MPa (see in Figure.2). In addition, a linear function of softening has been considered in current study in order to evaluate modeling of concrete in tension. The fracture energy method was used to specify the tension behaviour of concrete.  $G_f$  is the area under the softening curve and it was assumed equal to 164.8 J/m<sup>2</sup> (0.09 N/mm) and 192.3 J/m<sup>2</sup> (0.105 N/mm) for  $f_{cu} = 25$  MPa and  $f_{cu} = 35$  MPa respectively ( see Figure.3.).

For definition of the damaged plasticity model, some specific parameters which have to be defined to describe the non-linear behavior of concrete were assumed. Table 1 illustrates the values which are chosen in this study for the damage parameters. Coefficient of the dilation angle ( $\beta$ ) is dependent on the concrete shear strength. Shear resistance of concrete was affected by properties of aggregates and the age of the concrete. Magnitude of  $\beta$  was assumed because the experiment of Mohamed et al. (2012) not illustrated any information about the specifications of the aggregates and age of the concrete. According to Rasoul (2012), the dilation angle can vary from  $0^\circ \leq \beta \leq 56.3^\circ$ . For normal concrete, the  $\beta$  is often a reasonable assumption between  $30^\circ$  and  $40^\circ$ . In this study, a parametric study has been performed for different dilation angles and tension softening function (see in Figure.3) to select an appropriate value for each of them in comparison with the experimental results.

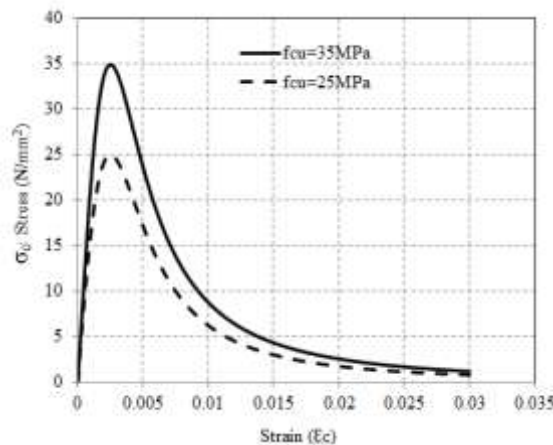


Figure.2 stress strain curve for concrete in compression.

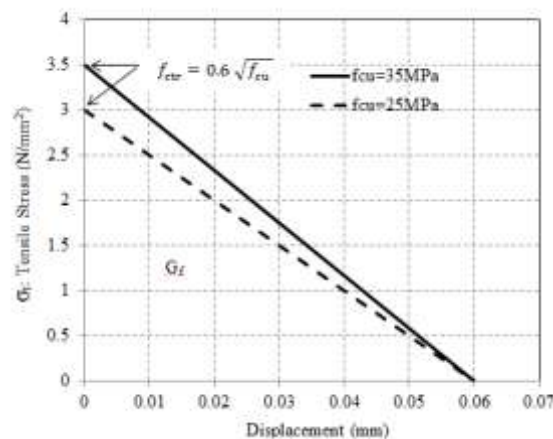


Figure.3 Tensile stress deformation relationship for concrete.

Table 1: Concrete damaged plasticity parameters

Dilation angle ( $\beta$ )	Eccentricity	$f_{b0} / f_{c0}$	K	Viscosity parameter
35	0.1	1.16	0.67	1E-07

4.1.2 Steel Reinforcement

The used reinforcement was represented as an elastic material in tension and compression. The assumed stress-strain curve of the steel bars is shown in Figure 4. Steel reinforced bars in the concrete were modeled as one-directional strain elements (truss element) and were simulated by T2D2 (A 2-node linear 2-D truss). It was obtained from experiment that the elastic modulus of steel ( $E_s$ ) was equal 200 GPa for all types of bars. For longitudinal bars in beam and column, the yield stress ( $f_y$ ) was measured in the experimental study and the value obtained was 400 MPa. While stirrups of both beam and column have a yield stress of 250 MPa. These values were used in the FEA model. A Poisson's ratio of 0.3 was used for the steel reinforcement. The bond between reinforcement bars and concrete was assumed as a perfect bond (embedded region). The material properties of reinforcement bars were assumed for the numerical simulation and it were listed in Table 2.



Figure.4. Stress strain behavior of steel.

Table 2: Material properties of reinforcement bars assumed for the numerical simulation.

a) D8mm bar	b) D16mm bar
*Material, Name= steel8	*Material, Name= steel16
*Elastic, Type = isotropic	*Elastic, Type = isotropic
200000, 0.30	200000, 0.30
*Plastic, Hardening=combined, Data type=parameters	*Plastic, Hardening=combined, Data type=parameters
250, 7993, 175	400, 7993, 175
c) D12mm bar	
*Material, Name= steel12	
*Elastic, Type = isotropic	
200000, 0.30	
*Plastic, Hardening=combined, Data type=parameters	
400, 7993, 175	

4.2. Numerical Analysis

2-Node linear elements (T2D2) were used for the reinforced concrete, reinforcement bars, and steel plates at supports in this model. Figure 5 shows finite element model of specimen for both concrete and steel. The boundary conditions and loading direction are illustrated in Figure 6. A fine mesh is needed to obtain results of sufficient accuracy. The mesh size is 25mmx25mm for all elements whether concrete or reinforcement. The processor type used for this study was intel(R) Core (TM) i3-2370 CPU @ 2.4GHz 2.4GHz.

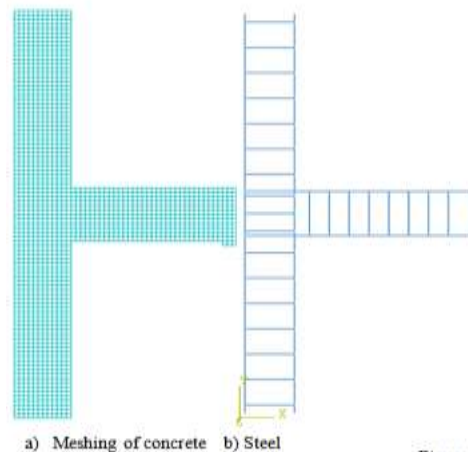


Figure 5. Finite element model of specimen.

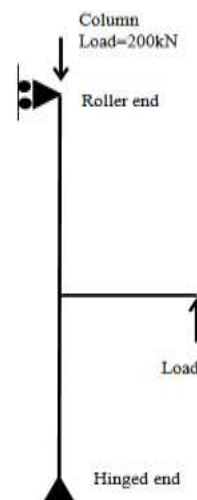


Figure 6 the boundary conditions and loading direction.

## V. Results

### 5.1. FEA Verification Of P-Δ Curve For control Tested Specimens (J0, JI0).

The Load–deflection (P-Δ) curve defined as the relationship between the applied force on free end of beam and vertical displacement at same point (see in Figure. 6). For the base control specimen (J0) shown in Figure.1, the free end beam deflection measured experimentally illustrated in Figure.7. Also the connection between beam and column was reinforced by three stirrups of 8mm diameter. The control specimen JI0 of group I was without joint reinforcement. Figure.8 shows Load–deflection (P-Δ) curve of control specimen JI0 obtained in experiment. After modeling for two control specimen J0 and JI0, the results showed in Figure 7 and Figure 8 respectively. There was a good agreement between FEM and experimental results for the two control specimens J0 and JI0 as shown in Figure 7 and Figure 8 respectively. The good agreement indicates that the models used for concrete and reinforcement can capture the fracture behaviour well. There are several possible causes for the differences between the experimental data and the finite element analysis. One is as for the control beam, the assumed perfect bond between concrete and steel reinforcement. In addition to, the stress- strain curve of concrete was not obtained from experimental work but it was estimated as mentioned previously in section 4.1.1 (see in Figure 2).

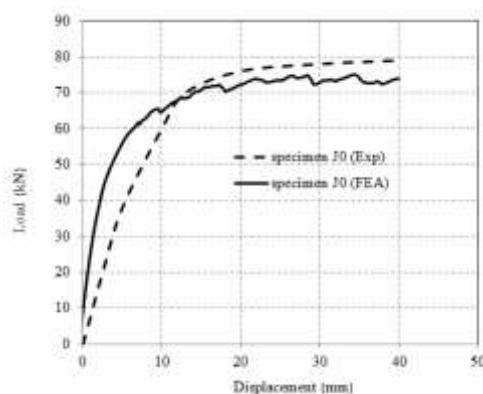


Figure .7 Load–deflection curve of Base control specimen J0, obtained by experiments and FEA (ABAQUS)

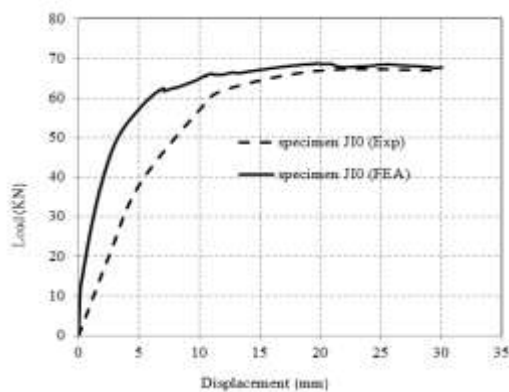


Figure.8 Load–deflection curve of control specimen JI0 of group I (without joint reinforcement), obtained by experiments and FEA (ABAQUS)

### 5.2. FEA verification of failure modes for specimens J0 and JI0.

The failure mode of base control specimen J0 and control specimen JI0 of group I using FEA just like in the experiments and this is illustrated in Figure. 9 and 10 respectively. For specimen J0, with joint reinforcement of 3D8mm, the failure mode was beam flexure as shown in Figure.9. This might be due to high resistance of the joint area. When the joint reinforcement of 3D8mm was removed in specimen JI0, the failure took place in the joint panel as shown in Figure.10. In the fact, the experimental work takes more time, effort, and high cost to reach conclusion. So, the modeling by ABAQUS program is useful and first to get accurate results in little time, and without cost. We could change joint reinforcement amount and joint reinforcement configuration and we studied its effect on the failure modes.

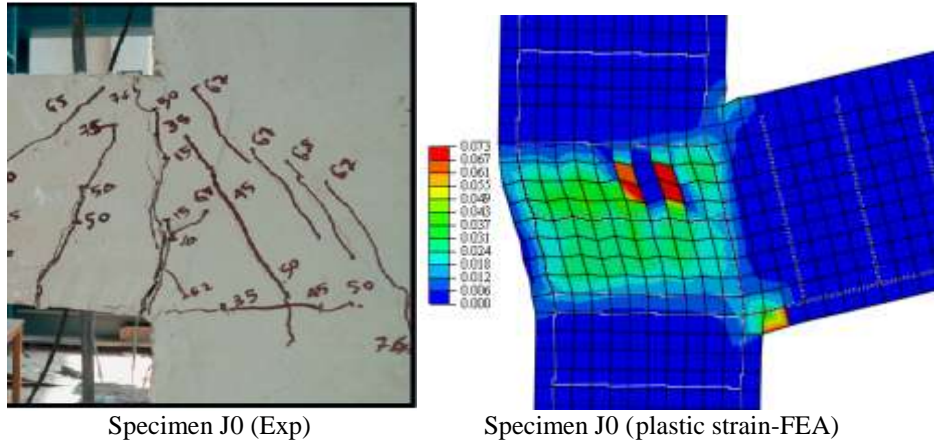


Figure.9 failure mode of Base control specimen J0, obtained by experiments and FEA (ABAQUS)

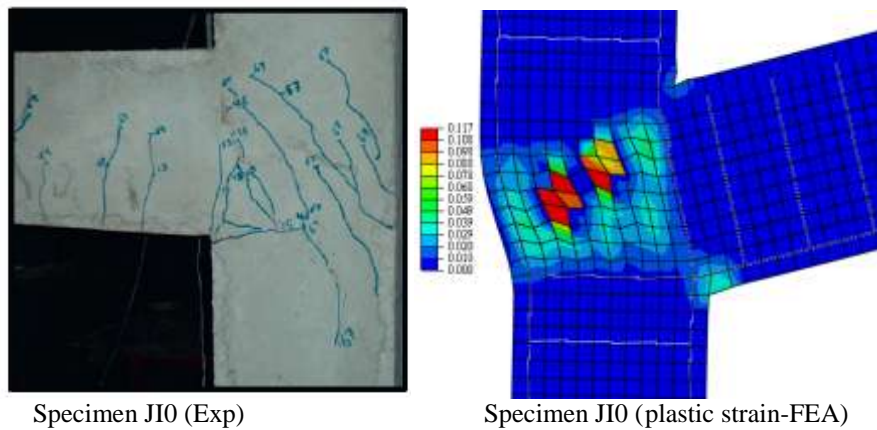


Figure.10 failure mode of control specimen J10 of group I (without joint reinforcement), obtained by experiments and FEA (ABAQUS)

### 5.3 Numerical Parametric Study.

Section 5.1 and 5.2 studied simulation of P-Δ curves and failure modes of control specimens JI, J10. It was obtained that the FEA results agreed with experiment results. So, three parameters were developed in the current study and its effect on load deformation behavior. The one is effect of axial column load while the second is effect of column width. The third is compressive strength of concrete.

#### 5.3.1 Effect of Column Width on Load Deformation Behavior

For base control specimen J0, with joint reinforcement, the column width was 200mm equal to beam width. The curve of load deformation was drawn by FEA as shown in Figure. 11. The column width was changed from 200mm to 250mm to 300 mm. the applied axial column load in test was 200 kN or 0.133  $A_g f_{cu}$ . So, the axial column load in FEA was dependent on cross-sectional area of column. On the other hand, the parameters of concrete compressive strength and column depth were constant. It must be noted that the column width have a big good effect on load deformation curve. As width of column increased, the capacity of beam column connection improved.

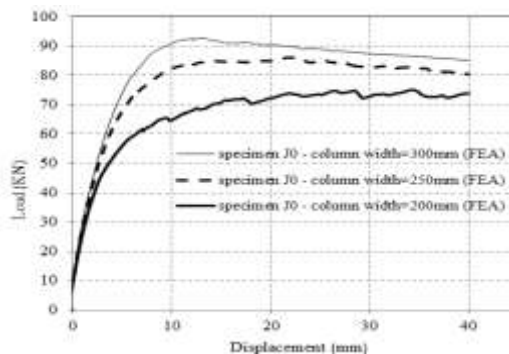


Figure.11 P-Δ curve of specimen J0 with different values of column width.

**5.3.2 Effect of Column Load on Load Deformation Behavior.**

Figure.12 shows P-Δ curve of specimen J0 in case of column width=250mm. Three values of axial column load of 200 kN, 250 kN, and 750 kN were applied. Although the value of column increased from 200 kN ( $0.107A_gf_{cu}$ ) to 750kN ( $0.40A_gf_{cu}$ ), the additional load at same displacement was not observed approximately. So, the axial column load has negligible effect on the behavior of the beam column connection as shown in Figure. 13. For assurance, the analysis were carried out using column width = 300 mm under column load of 240 kN and 300 kN. The results are shown in Figure. 13. The same conclusion was reached as well.

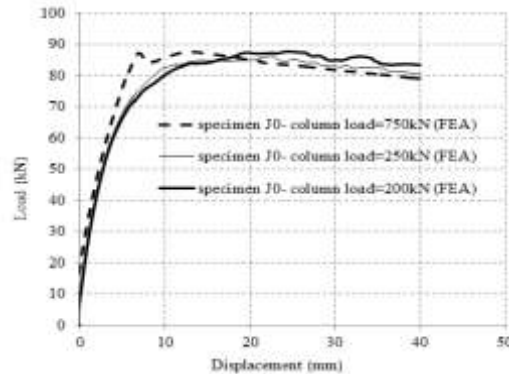


Figure.12 P-Δ curve of specimen J0 with different values of column load in case of column width=250mm.

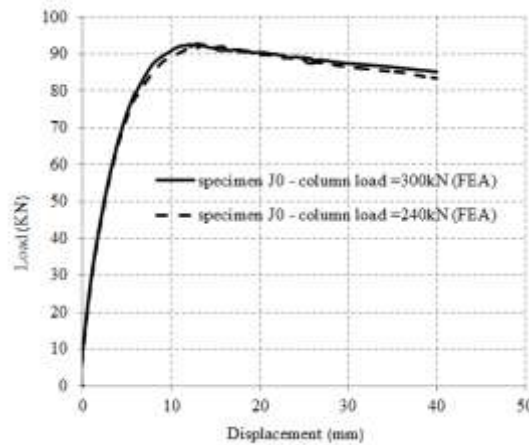


Figure13 P-Δ curve of specimen J0 with different values of column load in case of column width=300mm.

**5.3.3 Effect of Compressive Strength of Concrete on load Deformation Behavior.**

This section studied the effect of two degree of concrete 25 MPa and 35 MPa on the behavior of specimen J0. All details of specimen J0 showed in Figure.1. Only  $f_{cu}$  increased to 35 MPa. The stress strain curve of concrete with  $f_{cu} = 25$  MPa was drawn previously in figure 2. The concrete compressive strength affected on column capacity and beam flexure capacity hence affected on beam column connection. So, the compressive strength of concrete increased to  $f_{cu} = 35$  MPa and the stress strain curve drawn in figure 2 (As mentioned in section 4.1.1). This curve used in simulation. Also Modulus of elasticity  $E_c$  and tensile strength  $f_{ct}$  were calculated by Eq.(1) and Eq.(2) respectively. Figure.14 show the effect of compressive strength of concrete on behavior of beam column connection. It can be concluded that the compressive strength of concrete have a significant effect on the BCC behaviour. As compressive strength of concrete increased, the capacity of beam column connection improved.

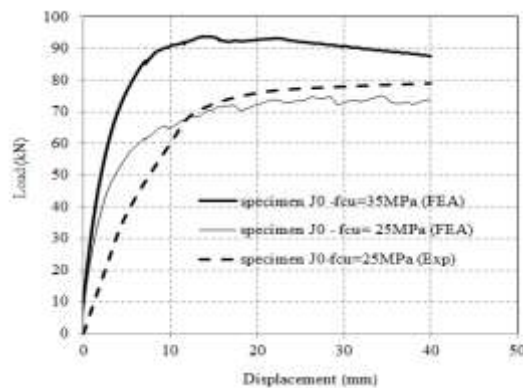


Figure 14 P-Δ curve of specimen J0 with different values of compressive strength of concrete.

## VI. Conclusion

The beam column connection is the most important structural element in reinforced concrete buildings. In the present study, a numerical investigation to the experimental work on the behavior of the beam column connection under static load was carried out. The effect of column load, column width and concrete compressive strength was studied. Based on the results of this investigation, the following conclusions or observations can be drawn:

- 1- There was a good agreement between finite element analysis (ABAQUS) and experimental results.
- 2- The failure modes of the beam column connection was classified to joint shear failure, slippage of the beam steel, beam flexure and yielding of the column main steel.
- 3- The beam flexure type of failure took place in case of specimens with joint shear reinforcement while the joint shear failure occurred in case of specimens without joint shear reinforcement.
- 4- The concrete compressive strength had a significant influence on the BCC behaviour.
- 5- The axial column load ratio had a negligible effect on the BCC behaviour.
- 6- The increase of column width in perpendicular direction on the beam improved the behavior of the beam column connection.

## References

- [1] ABAQUS Version 6.9, "SIMULIA Products", Documentation Web site: <http://www.engine.brown.edu:2080/v6.7/index.html>. Last accessed: September 2009.
- [2] Davide Buzzini, dipl. Bau-Ing. ETH "Quasi-Static Cyclic Tests on three hybrid Fibre Concrete Structural Walls" Institute of Structural Engineering, Swiss Federal Institute of Technology, phd thesis, 2006.
- [3] Egyptian Code for Design and Construction of Reinforced Concrete Structures, (ECP 203-2007) 2012.
- [4] Hu H-T, Schnobrich WC. Constitutive modelling of concrete by using Nonassociated plasticity. *J Mater Civil Eng (ASCE)* 1989;1(4):199–216.
- [5] Hibbitt, Karlsson, and Sorensen, Inc. ABAQUS Theory manual, User manual and Example Manual, Version 6.7. Providence, RI; 2000.
- [6] Fu, J., Chen, T., Wang, Z., and Bai, S., (2000), "Effect of axial load Ratio on seismic behaviour of interior beam-column joints", the 12<sup>th</sup> World conference of earthquake engineering, Paper No. 2707.
- [7] Kiran, R., and Genesio, G., (2014), "A case study on pre 1970s Constructed concrete exterior beam-column joints", *Case Studies in Structural Engineering*, Vol.1, pp. 20–25.
- [8] Mohamed H. Mahmoud, Hamdy M. Afefy, Nesreen M. Kassem, Tarek M. Fawzy "Strengthening of defected beam-column joints using CFRP" Cairo University, *Journal of Advanced Research*, Vol.5, P:67-77, 2014.
- [9] Murakami, H., Fujii, S., Ishiwata, Y., and Morita, S., (2000), "Shear Strength and deformation capacity of interior RC beam-column joint subassembly", the 12<sup>th</sup> world conference of earthquake Engineering, Paper No. 679.
- [10] Park, S., and Mosalam, K. M., (2012), "Parameters for shear strength Prediction of exterior beam-column joints without transverse Reinforcement", *Engineering Structures*, Vol. 36, pp. 198–209.
- [11] Rasoulnilforoushamedani "numerical evaluation of structural behavior of the simply supported FRP- RC beams" Master of science thesis, Stockholm Sweden, 2012.
- [12] Saenz, LP. Discussion of "Equation for the stress-strain curve of concrete" by Desayi P, Krishnan S. *ACI Journal* 1964;61:1229–35.
- [13] Yasmeen Taleb Obaidat, Susanne Heyden, Ola Dahlblom "The effect of CFRP and CFRP/concrete interface models when modeling retrofitted RC beams with FEM" *journal of Composite Structures*, Vol. 92 PP. 1391–1398, 2010.